



UNIVERSITY  
OF HULL

**CATAPULT**  
Satellite Applications

**CATAPULT**  
Offshore Renewable Energy



# Novelties for the offshore wind profile

*WindSim user meeting 2019*

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- Introduction
- Review of  $z_0$  methodologies
- On offshore high  $z_0$  values
- Development of a new formulation
- Sensibility analysis
- Conclusions
- Further development

# Introduction: The WindRes project

## Aim of the project

Develop a tool providing information on wind resource for a targeted site using wind observations from space

## Key challenges

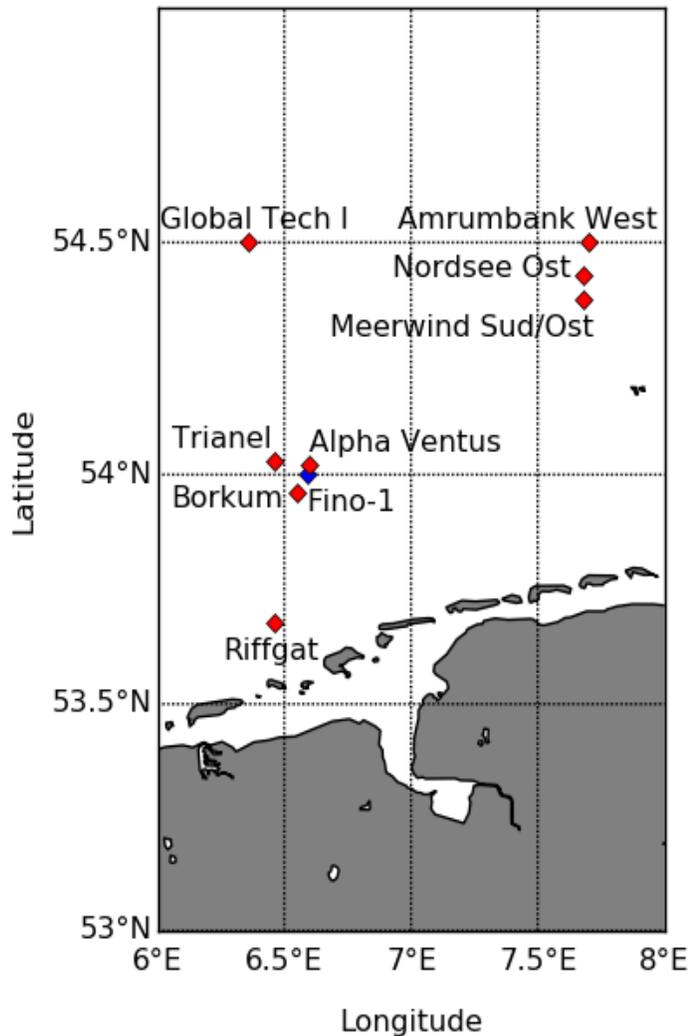
Translate NORSEWInD research into commercial, operational tools.

Develop key applications for offshore renewable energy industry and demonstrate its impact.

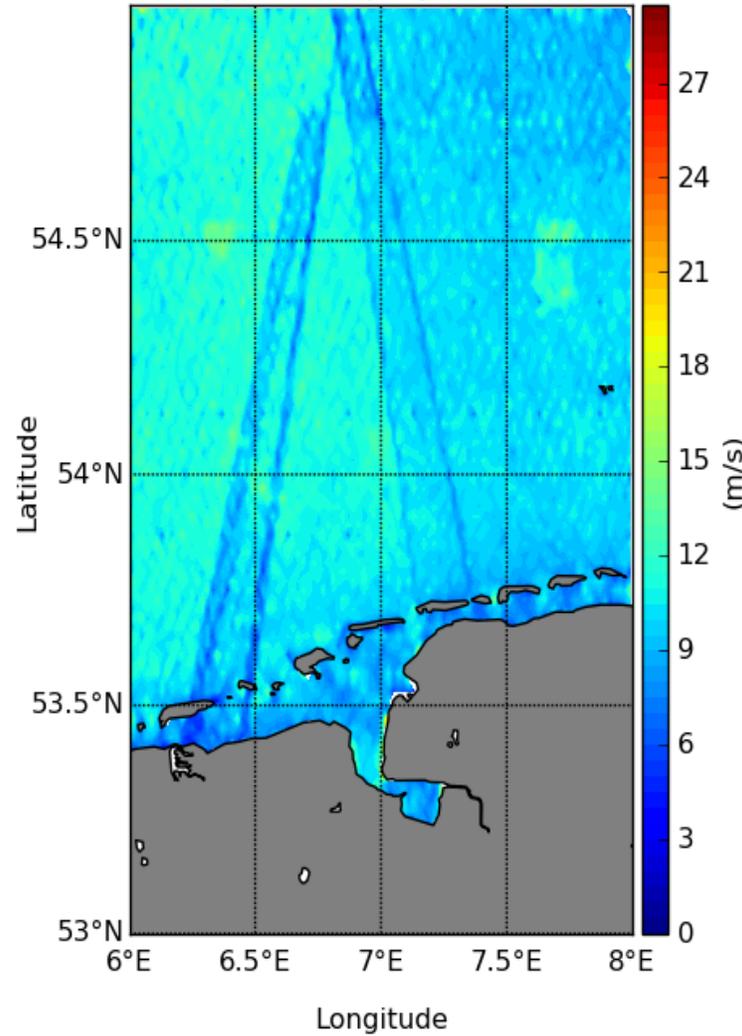
Demonstrate opportunities offered by satellite services within energy sector.

# Introduction: The WindRes project

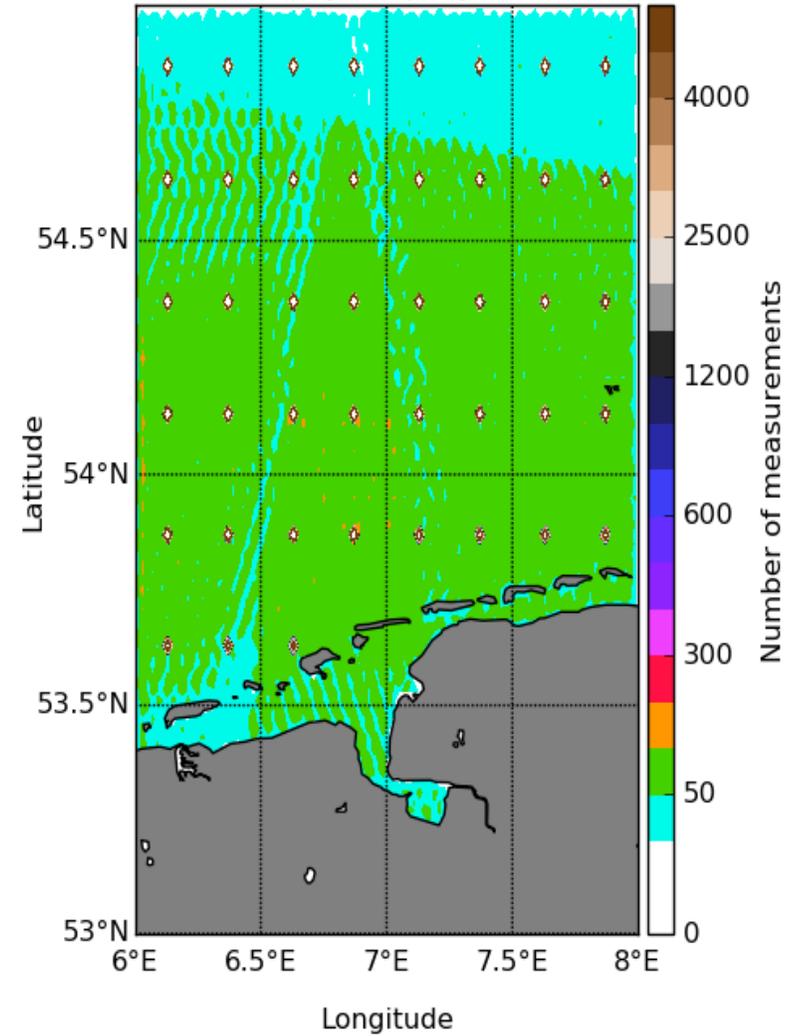
Location



Wind speed map

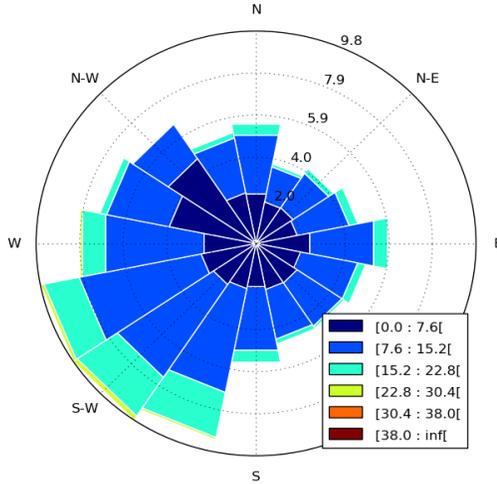


Data density map

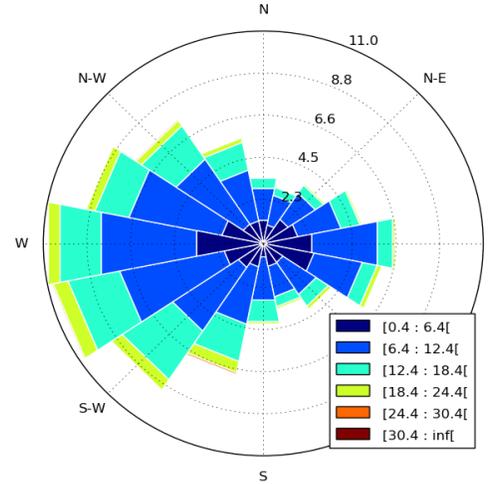


# Introduction: The WindRes project

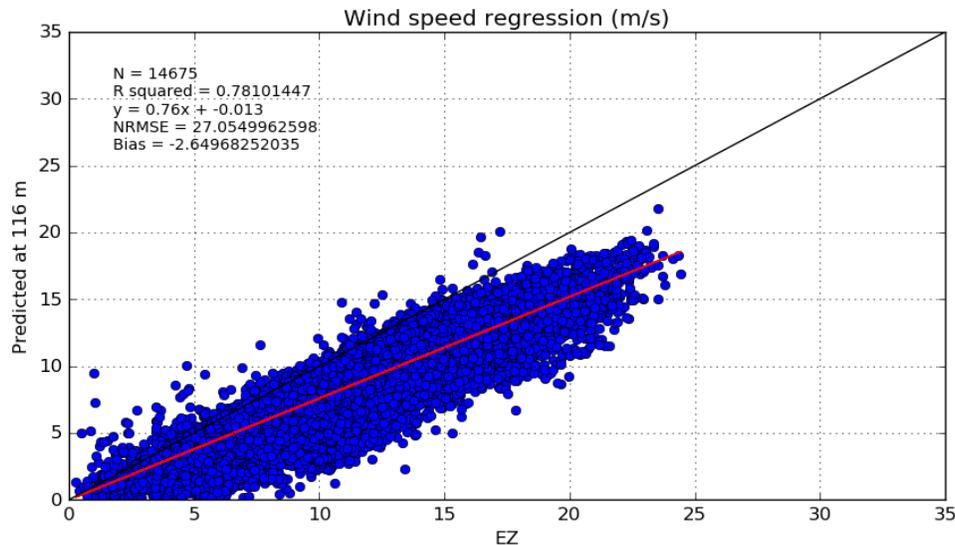
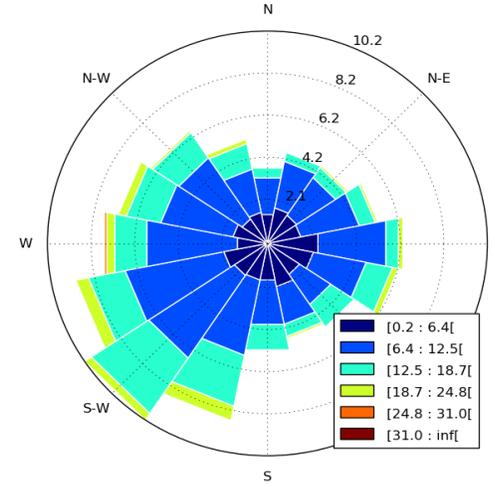
Wind statistics at 100m and at 6.59/53.99 during 01/01/2004:30/11/2011 by fino1\_clean.xlsx



Wind statistics at 100m and at 6.63/54.13 during 2004-01-01:2011-11-30 by Quikscat



Wind statistics at 100m and at 6.63/54.13 during 2004-01-01:2011-11-30 by ASCAT



Open source code available on GitHub:

<https://github.com/SatelliteApplicationsCatapult/WindRes>

# Introduction: The WindRes project

## Difficulties

- Time between measurements
- Vertical extrapolation of wind speed
- Coastal areas
- Truncation of wind speed distribution
- Low accuracy for low and high winds
- Criteria for image processing

## Influences

- Weather (rain, water column)
- Marine atmospheric boundary layer
- Surface waves
- Internal waves
- Currents
- Bathymetry
- Surface slicks

## Opportunities for the wind sector

- Use of satellite data as historical data during the MCP method (**planning stage**)
- GNSS-Reflectometry for real time measurements (**construction & operation stages**)

# Introduction: Vertical extrapolation

$$U(z) = \frac{U_*}{k} \left[ \ln \left( \frac{z}{z_0} \right) + \Psi_s(z/L_s) \right] \quad z \gg z_0$$

Rewritten equation

$$U(z) = \frac{U_*}{k} \left[ \ln \left( \frac{z}{z_0} \right) - \Psi_m \right]$$

$$U(z) = \frac{U_*}{k} \left[ \ln \left( \frac{z}{z_0} \right) \right]$$

Neutral winds at 10 m over the sea



2 measurements at different heights required

~~$$U(z) = U(z_r) \left[ \frac{\ln(z/z_0)}{\ln(z_r/z_0)} \right]$$~~

Charnock's equation

$$z_0 = \alpha_c \frac{U_*^2}{g}$$

$z_0$   
 $U_*$

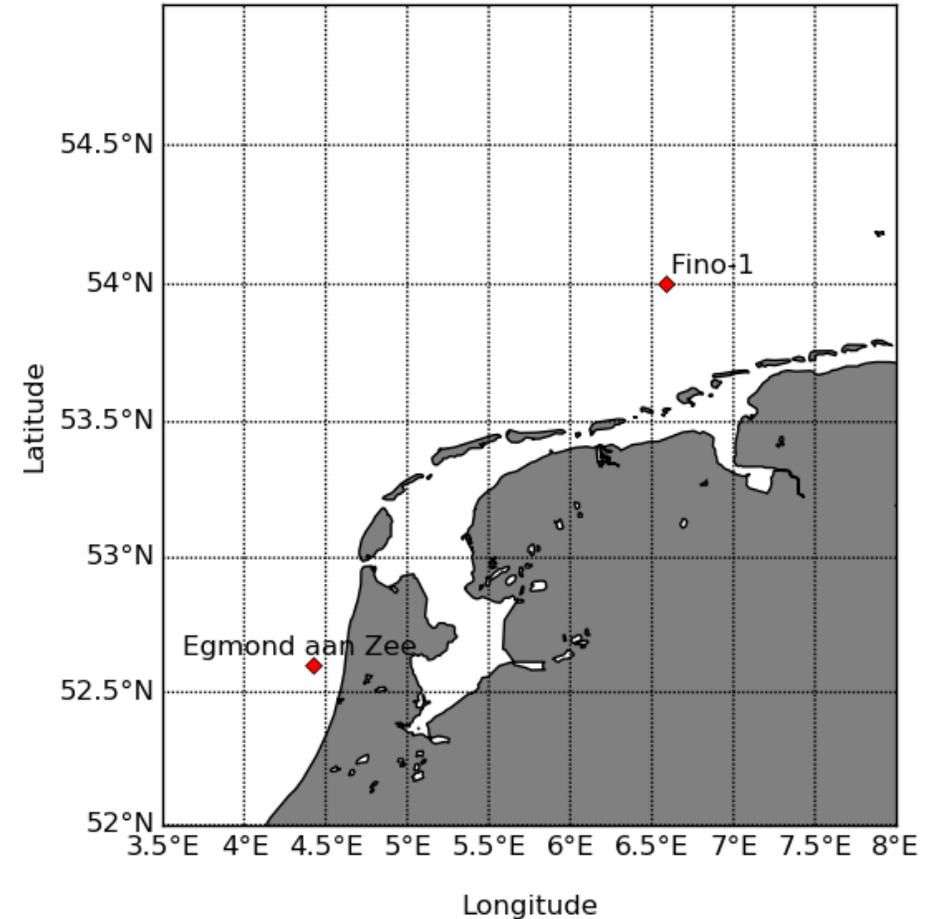


- $U$ : wind speed
- $U_*$ : friction velocity
- $k$ : von Karman constant
- $z$ : height
- $z_0$ : surface roughness length
- $\Psi$ : atmospheric stability correction
- $L_s$ : Obukhov length
- $\alpha_c$ : Charnock's parameter
- $g$ : gravitational acceleration

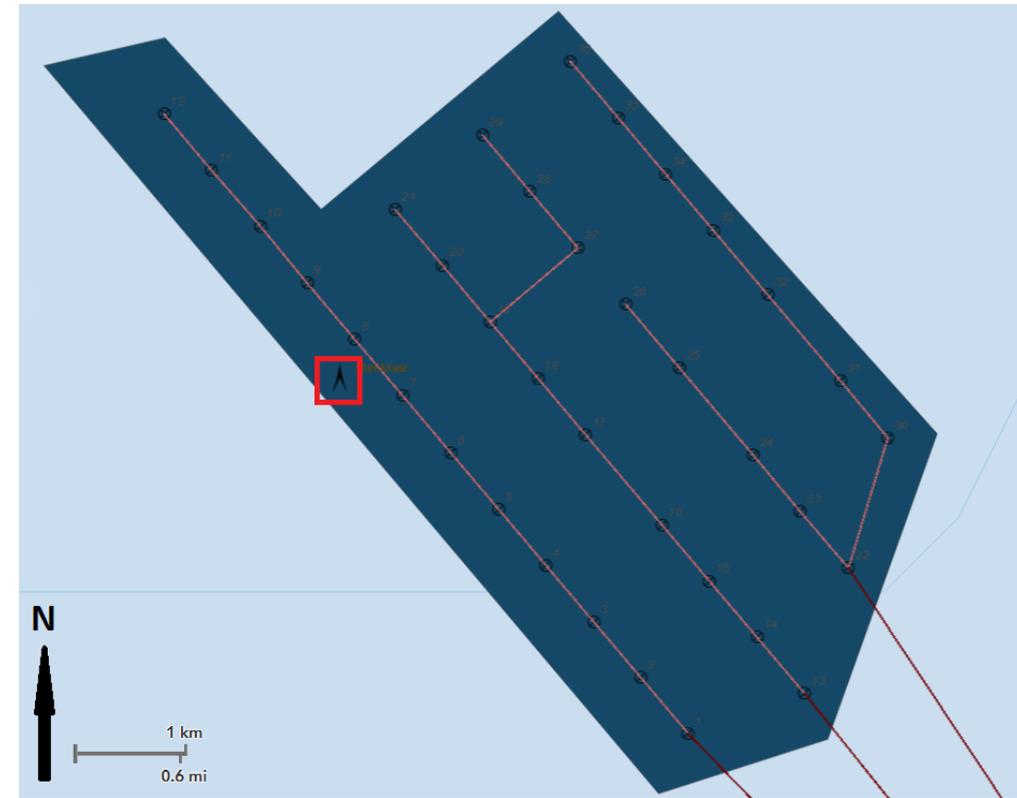
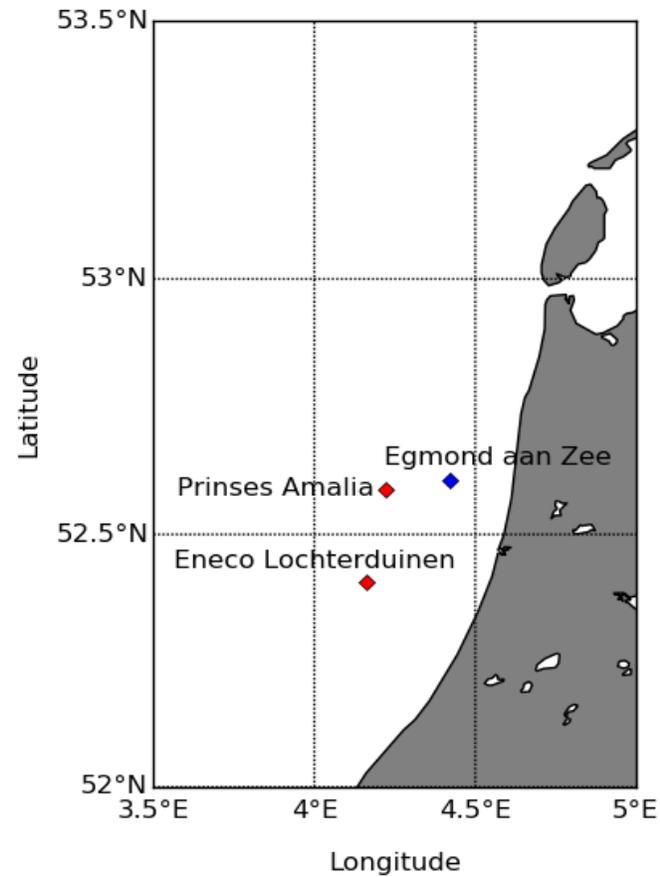
# Introduction: Locations

In situ data composed by two meteorological masts in the North Sea, Fino-1 & Egmond aan Zee.

	Fino-1	Egmond
Distance to shore	40 km	14.5 km
Depth	30 m	16.5 m
From	1/1/04	1/7/05
To	30/11/11	31/12/08
Highest anemometer	90 m	116 m



## Egmond aan Zee



Source: [www.4coffshore.com](http://www.4coffshore.com)

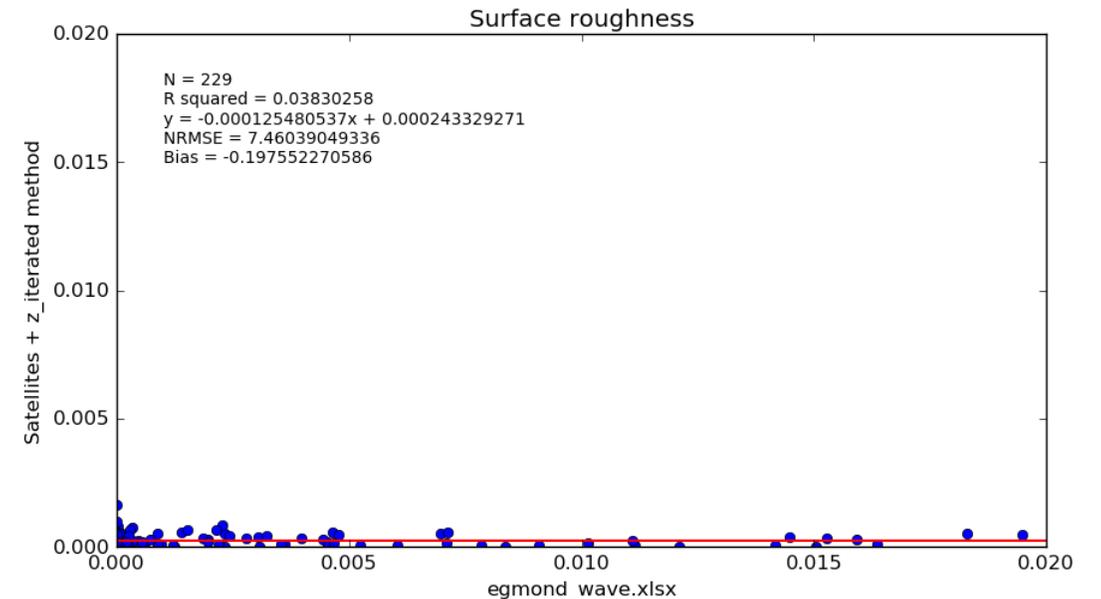
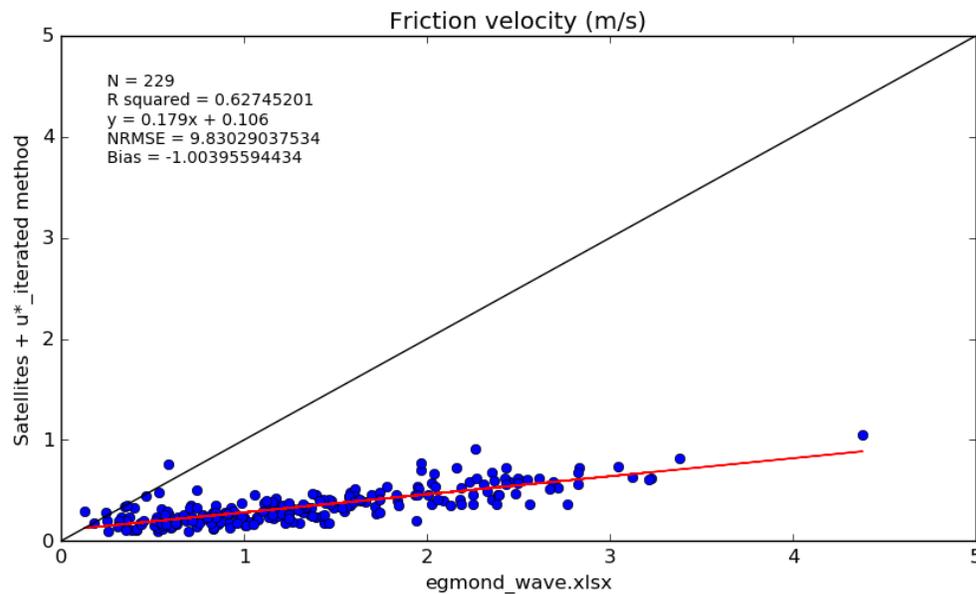
# Review of $z_0$ methods: Constant $\alpha_c$

$$U(z) = \frac{U_*}{k} \left[ \ln \left( \frac{z}{z_0} \right) \right]$$



$$z_0 = \alpha_c \frac{U_*^2}{g}$$

1. Constant Charnock's parameter,  $\alpha_c = 0.0144$
2. Calculate  $U^*$  and  $z_0$  at 10 m
3. Calculate  $U$  when  $z$  is the hub height



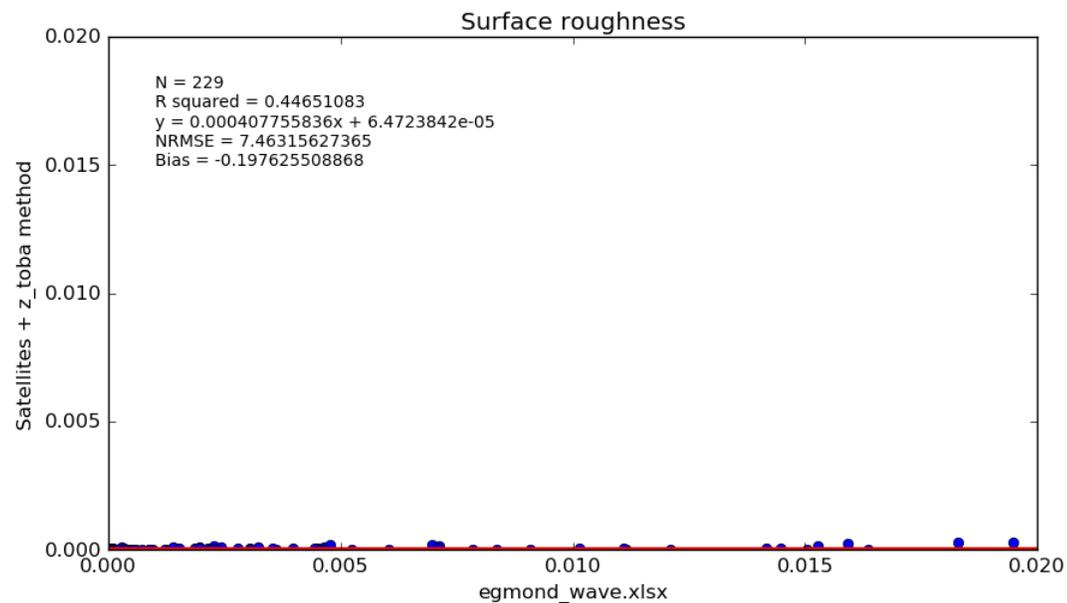
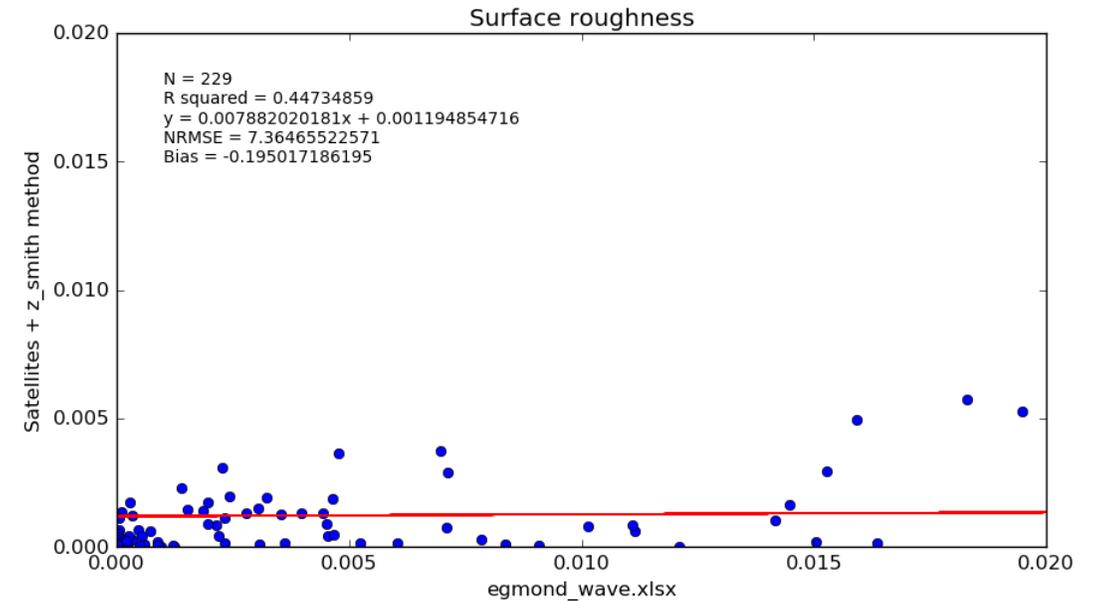
# Review of $z_0$ methods: Wave age expressions

$c_p$ : phase speed of the wave

$c_p/u_*$ : wave age

Smith

$$\alpha_c = 0.48(u_*/c_p)$$



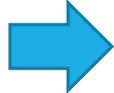
Toba

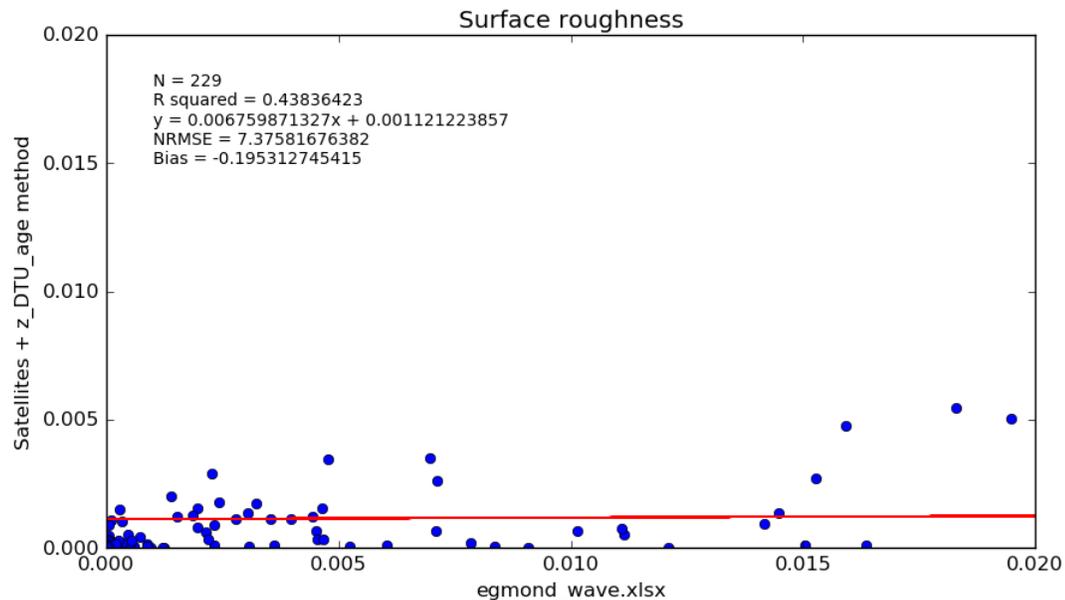
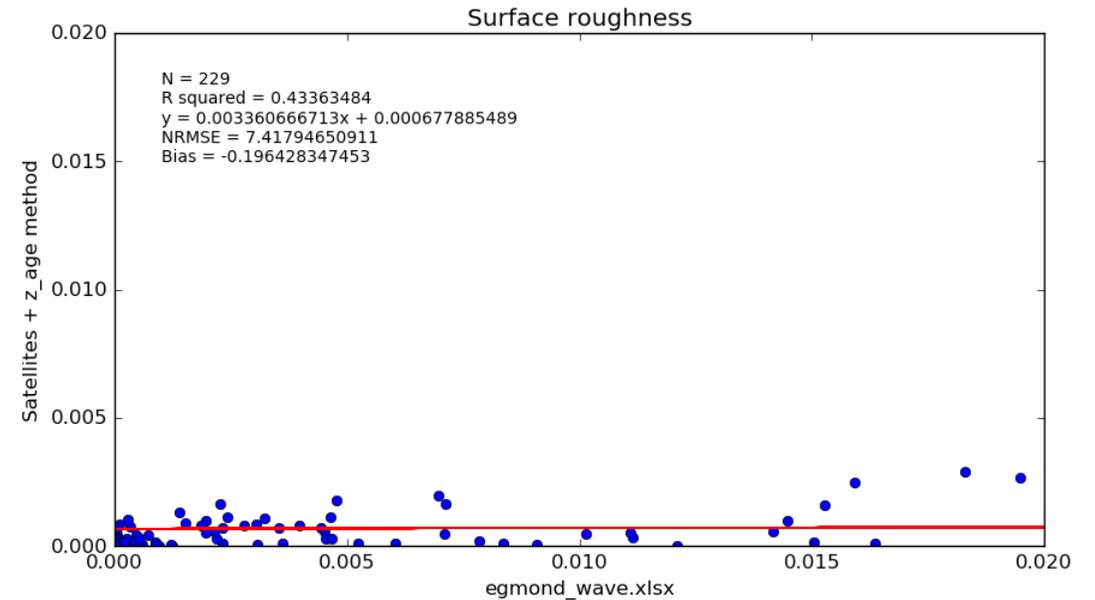
$$\alpha_c = 0.025(u_*/c_p)$$



# Review of $z_0$ methods: Wave age expressions

Edson

$$\alpha_c = 0.114 \left( \frac{u_*}{c_p} \right)^{0.622}$$




Astrup



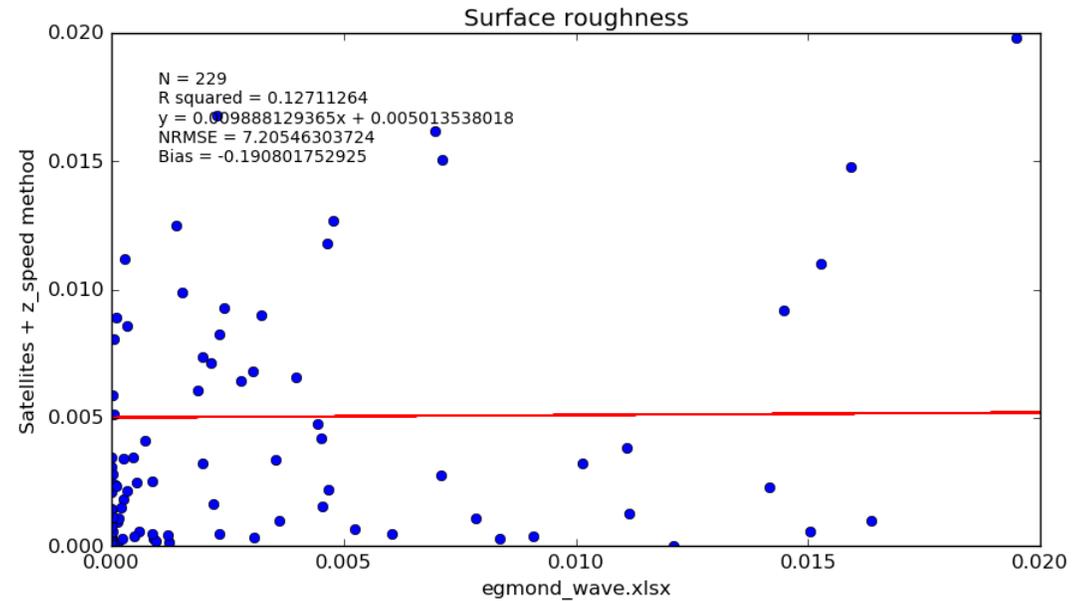
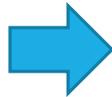
$$\alpha_c = 1.89 \left( \frac{u_*}{c_p} \right)^{1.59}$$

$$\times \left[ 1 + 47.165 \left( \frac{u_*}{c_p} \right)^{2.59} + 11.791 \left( \frac{u_*}{c_p} \right)^{4.59} \right]^{-1}$$

# Review of $z_0$ methods: Wind speed expressions

Edson

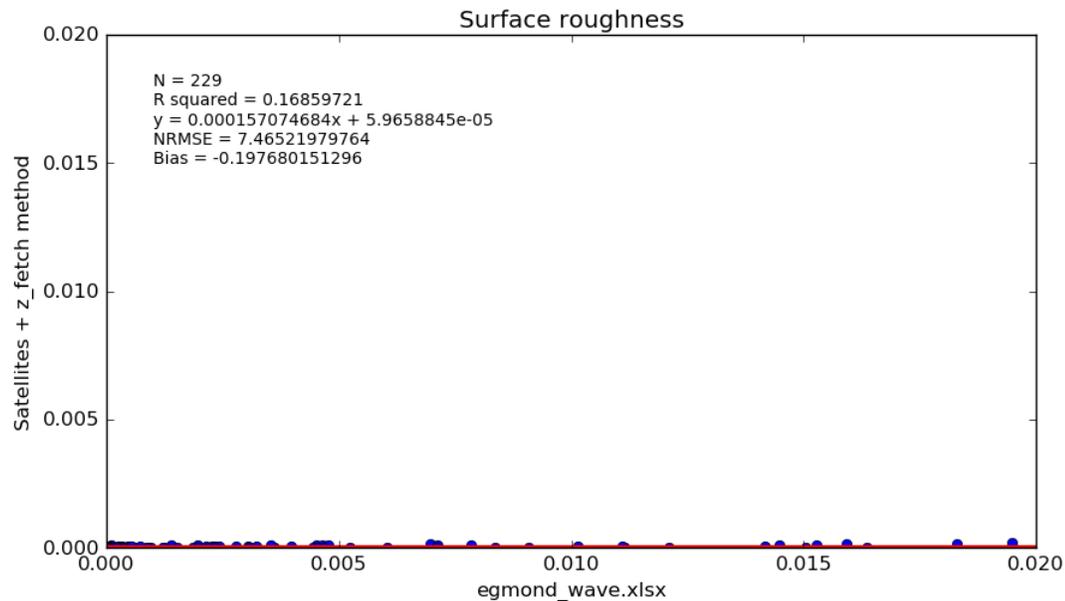
$$\alpha_c = 0.017U_{10N} - 0.005$$



Astrup

$$\frac{u_*}{c_p} = \frac{3.5}{2\pi} \times \left( \frac{(U_{10})^2}{x \times g} \right)^{1/3}$$

$x$  : fetch



# Review of $z_0$ methods: Wave slope expressions

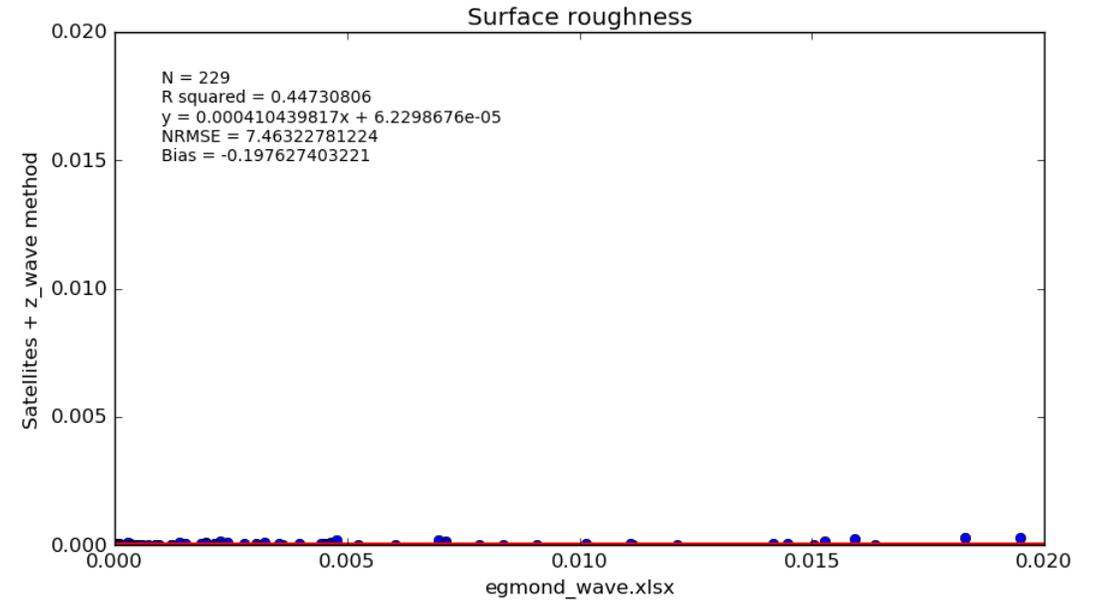
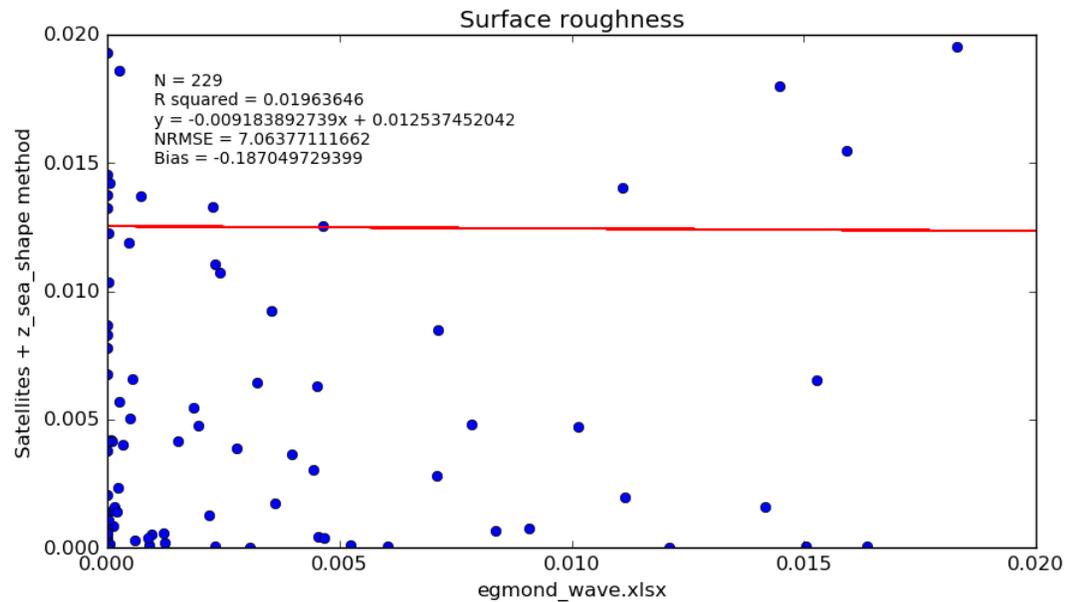
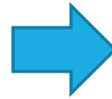
$H_s$  : significant wave height

$L_p$  : wave length

$H_s/L_p$  : wave slope

Edson

$$\alpha_c = 0.09H_s \left( \frac{2\pi}{L_p} \right)$$

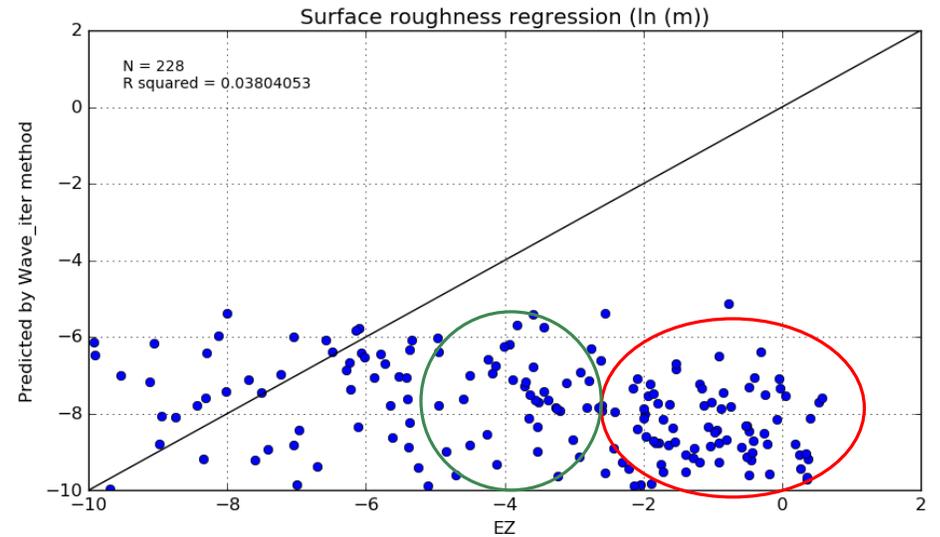
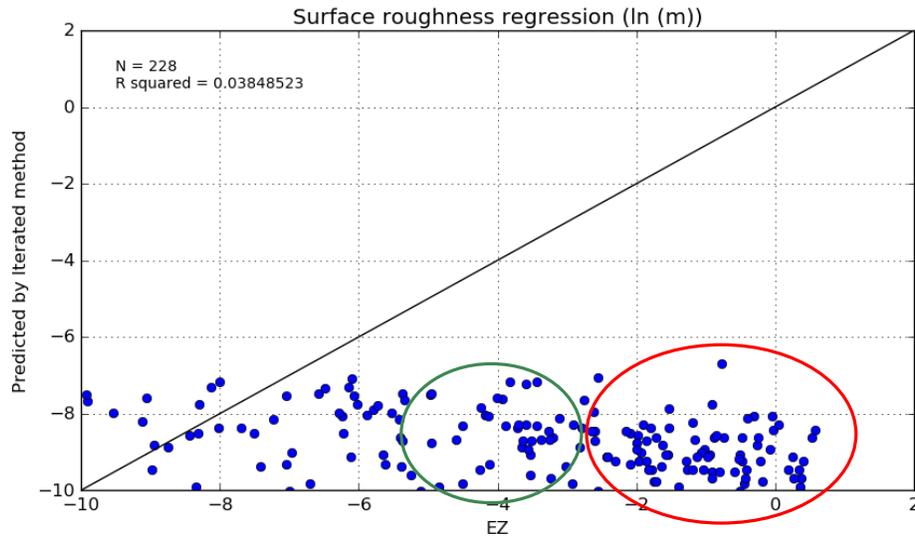


Taylor

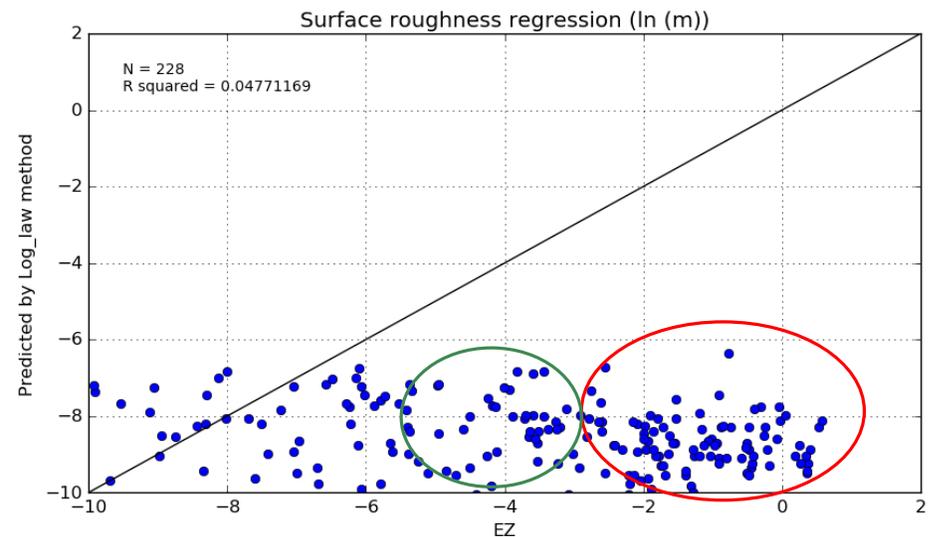
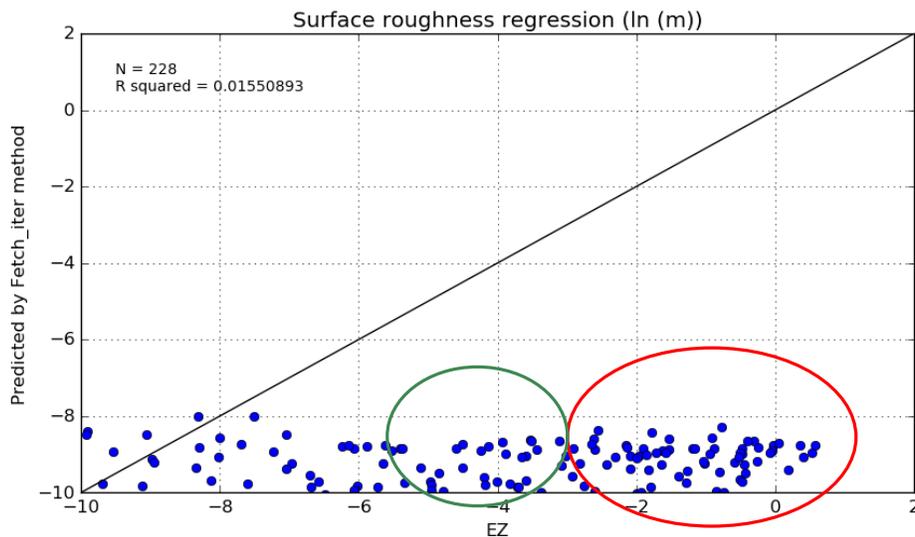


$$\frac{z_0}{H_s} = 1200(H_s/L_p)^{4.5}$$

# Review of $z_0$ methods: Log scale

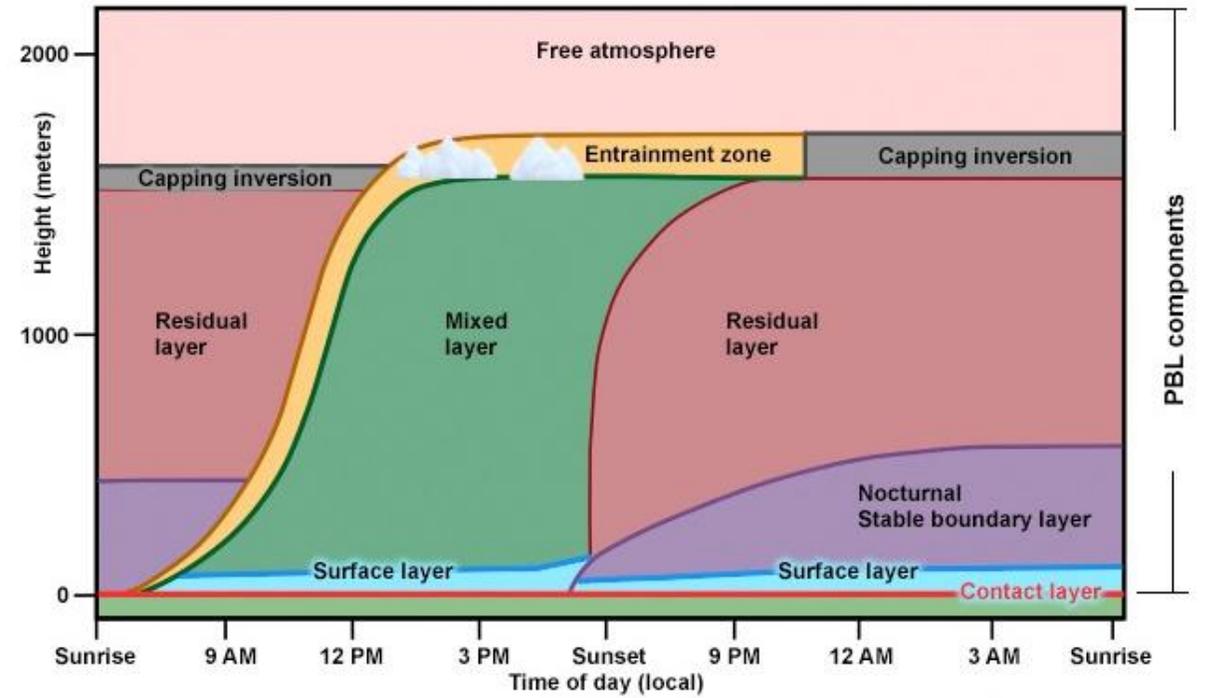


Offshore  $z_0$   
 $\sim 10^{-3} - 10^{-5}$  !!!



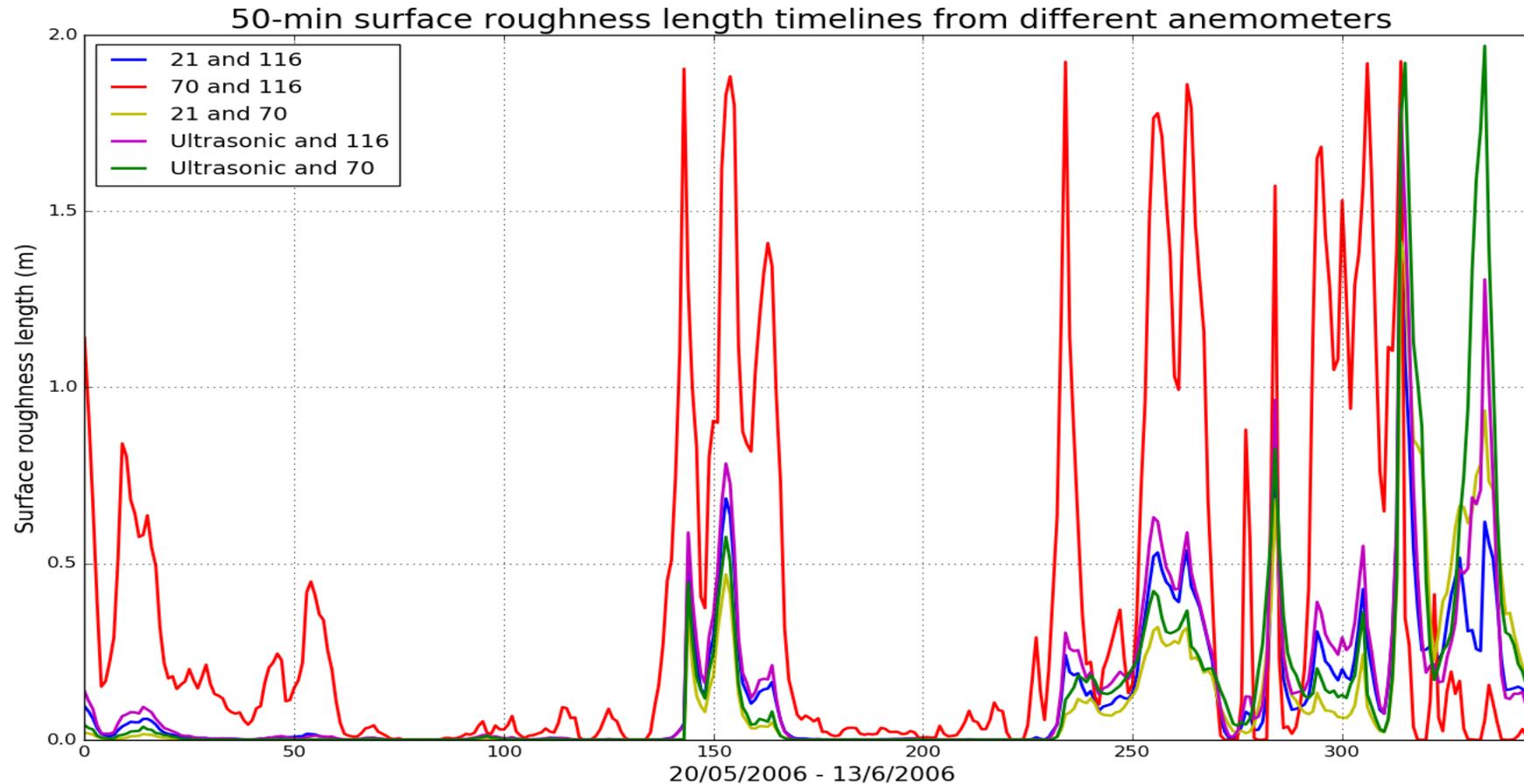
## Possible Reasons

- Instrumental errors ( anemometers, vanes, datalogger,...)
- Physical phenomena ( wind shear, eddies, low-level jets )
- Atmospheric stability ( heat flux or turbulence )
- Wake effect ( WT's nearby or other obstacles )
- Incomplete physical law ( log law and/or  $z_0$  model )



Source: MetEd UCAR

# On offshore high $z_0$ values: Instruments

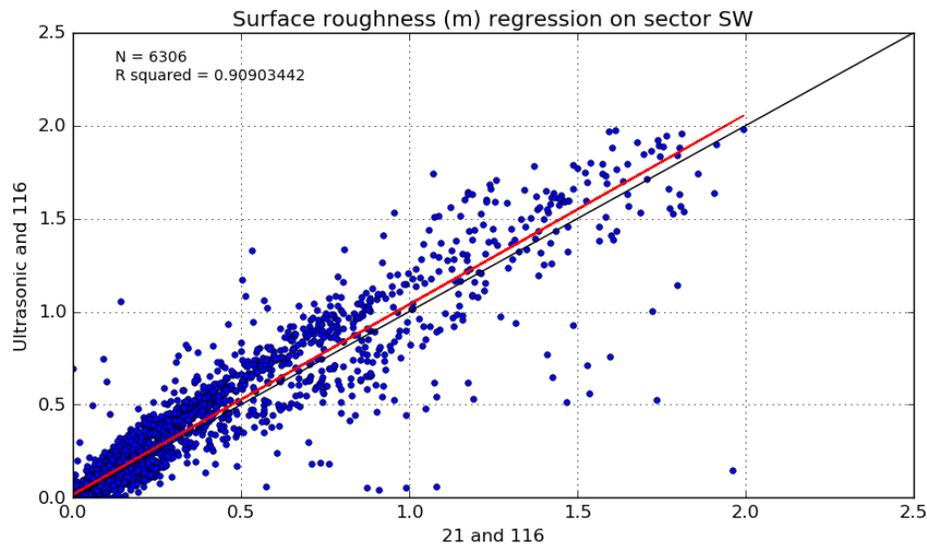
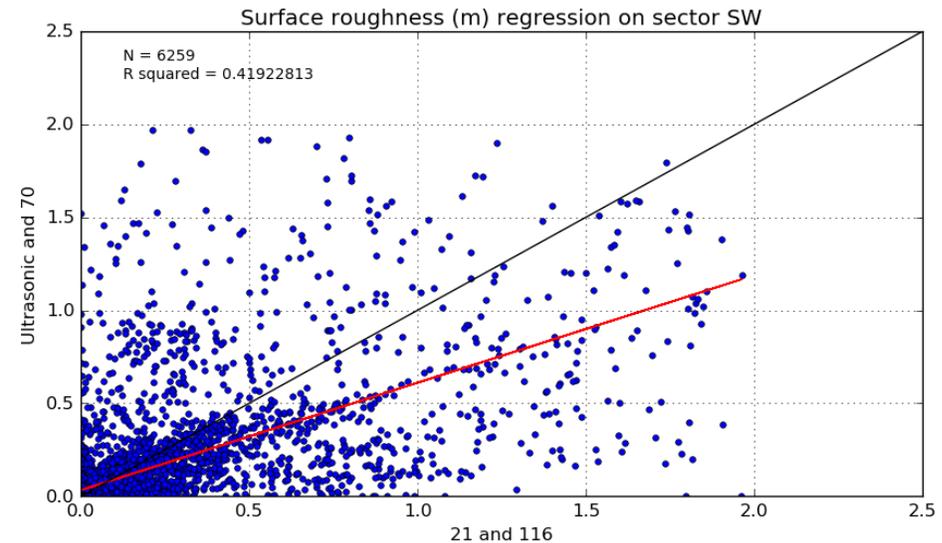
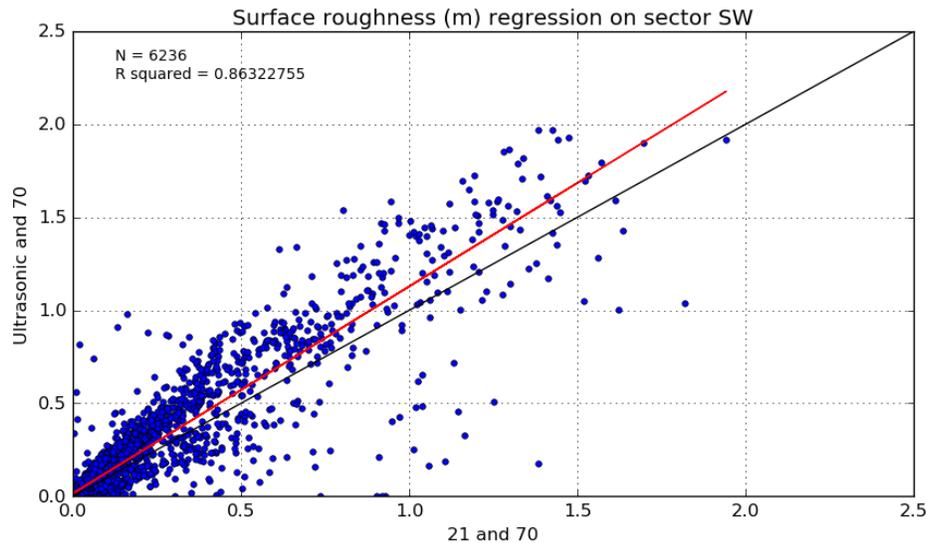


$$U(z) = U(z_r) \left[ \frac{\ln(z/z_0)}{\ln(z_r/z_0)} \right]$$

Egmond aan Zee:

Cup anemometers at  
21, 70, 116 meters  
Sonic anemometer at  
21 meters

# On offshore high $z_0$ values: Instruments



It seems to be certain disagreement between anemometers at 70 and 116 metres. However, high  $z_0$  was always found

# On offshore high $z_0$ values: Phenomena

**Gusts, eddies and wind shear** can be significant for periods of 10 minutes or less. Hence, 50 minutes periods were used.

**Low-level jets** use to be larger in time than eddies. These could be represented as an inverted wind profile, lower wind speed at high heights than low heights. In these cases, the  $z_0$  cannot be mathematically calculated by the logarithmic law; and then these situations were filtered out.

# On offshore high $z_0$ values: Stability

$$\Theta_v = \Theta(1 + 0.61r)$$

$$L_s = -\frac{u_*^3 \Theta_v}{\kappa g \overline{w' \Theta'_v}}$$

$\Theta$  : Potential temperature

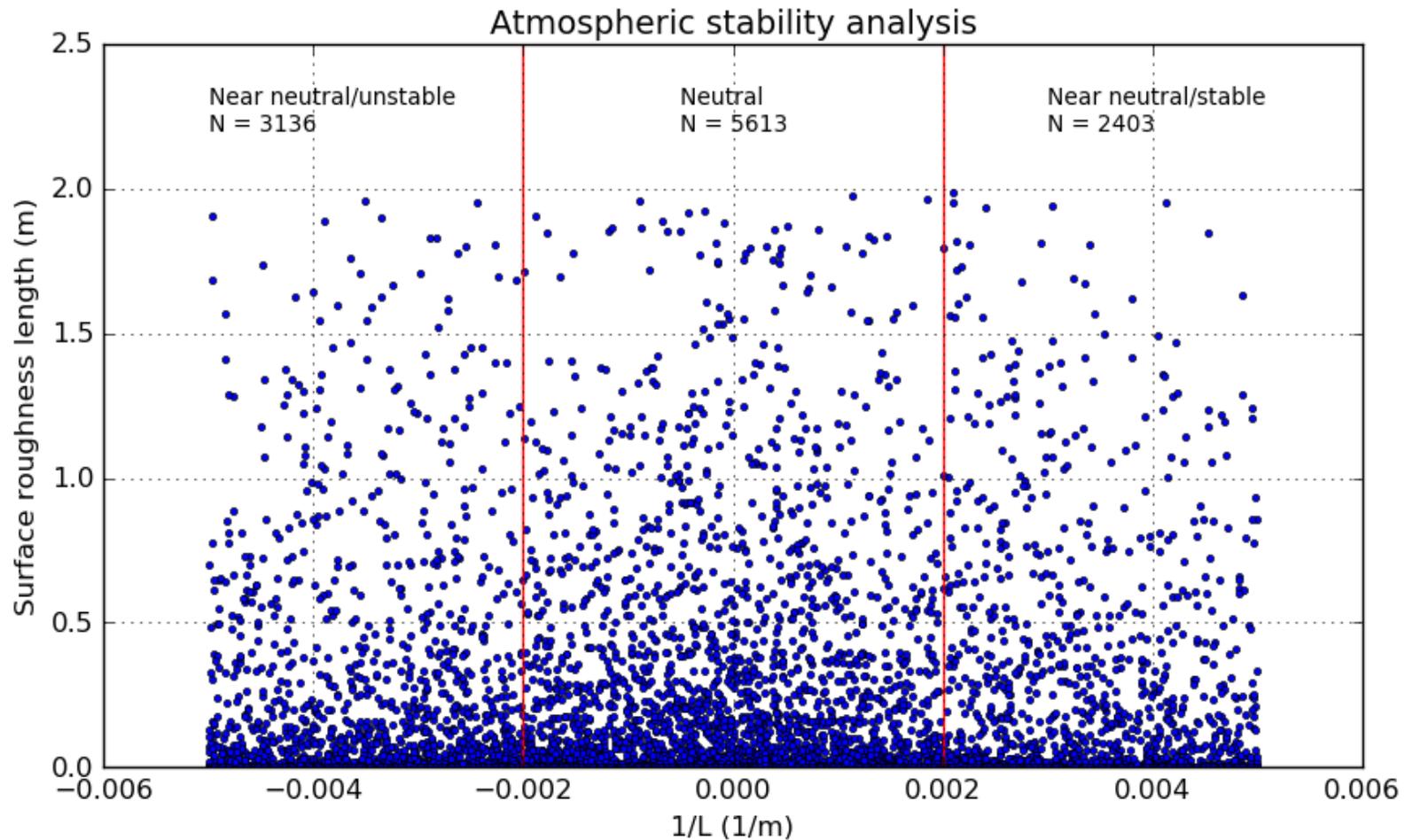
$\Theta_v$  : Virtual potential temperature

$w'$  : vertical speed

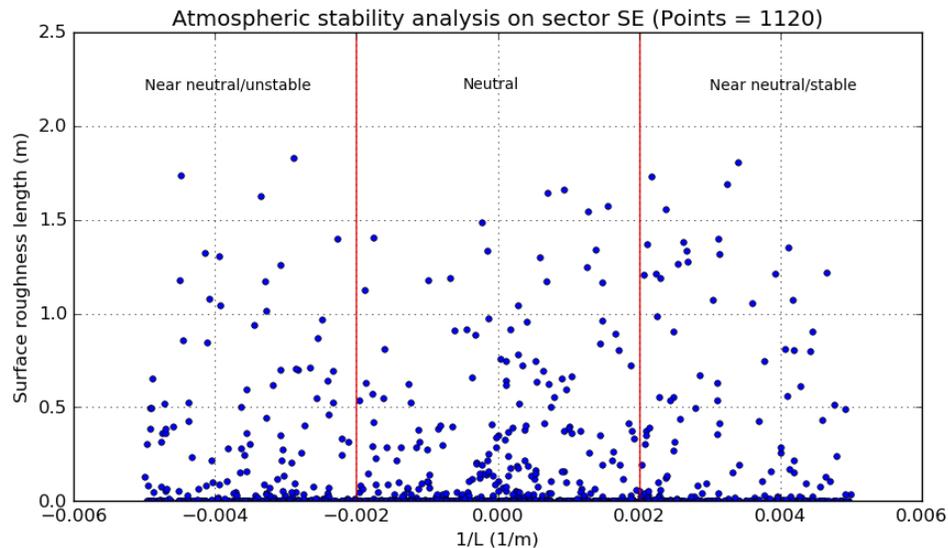
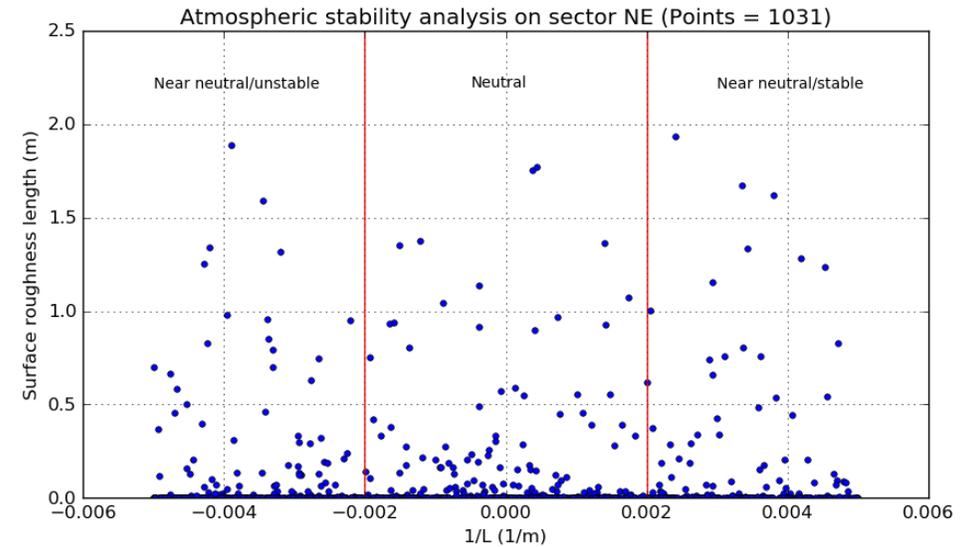
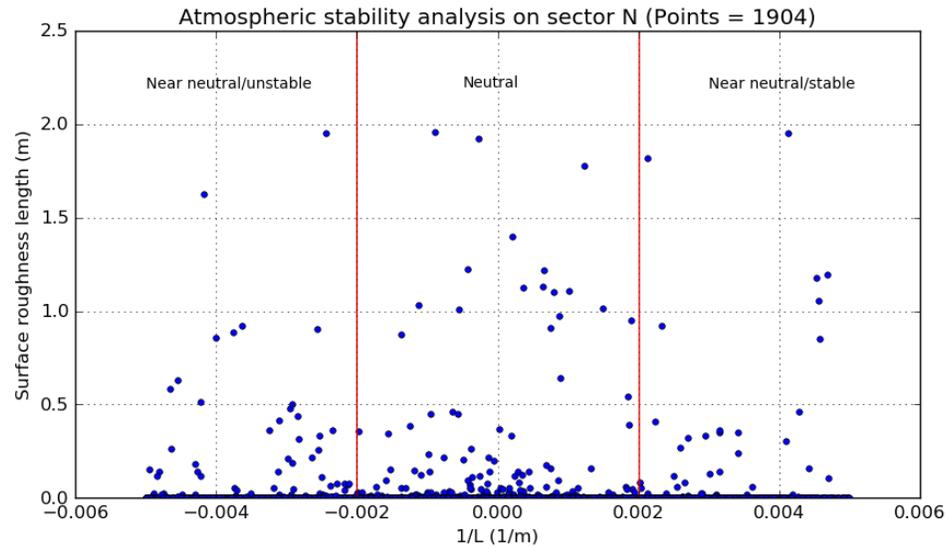
$\overline{w' \Theta'_v}$  : Heat flux

		$\overline{\Theta}_v$ profile (K)	$\overline{w' \Theta'_v}$ (ms <sup>-1</sup> K)	$z/L_s$	$L_s$ (m)	$1/L_s$ (m <sup>-1</sup> )
<b>Stable</b>		$\overline{\Theta}_{v1} < \overline{\Theta}_{v2}$	< 0	> 0	$\leq 200$	$\geq 0.005$
<b>Neutral</b>	<b>Near neutral/stable</b>	$\overline{\Theta}_{v1} \cong \overline{\Theta}_{v2}$ If there is no convection	$\cong 0$	$\cong 0$	$200 \leq L \leq 500$	$0.002 < 1/L < 0.005$
	<b>Neutral</b>				$ L  \geq 500$	$0.002 \geq 1/L \geq -0.002$
	<b>Near neutral/unstable</b>				$-500 \geq L \geq -200$	$-0.005 \leq 1/L \leq -0.002$
<b>Unstable</b>		$\overline{\Theta}_{v1} > \overline{\Theta}_{v2}$	> 0	< 0	$\geq -200$	$\leq -0.005$

# On offshore high $z_0$ values: Stability

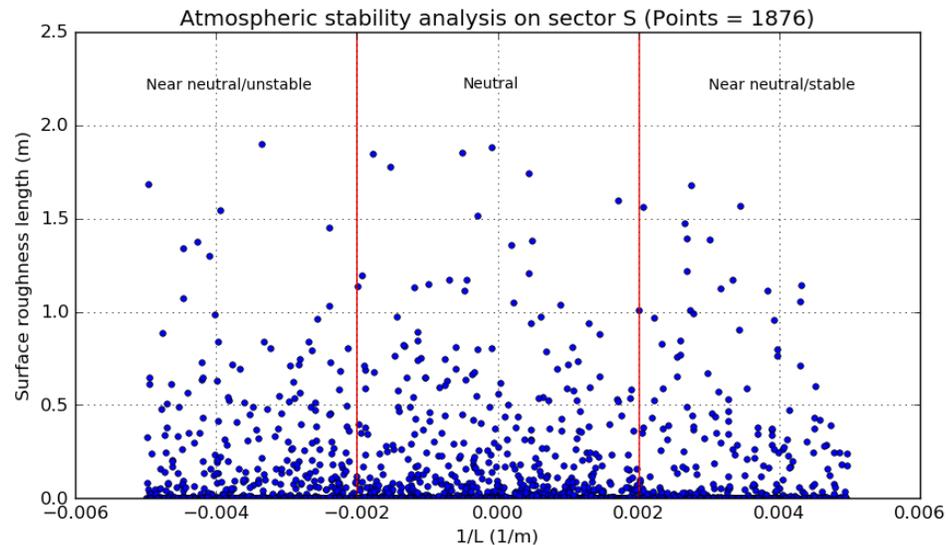
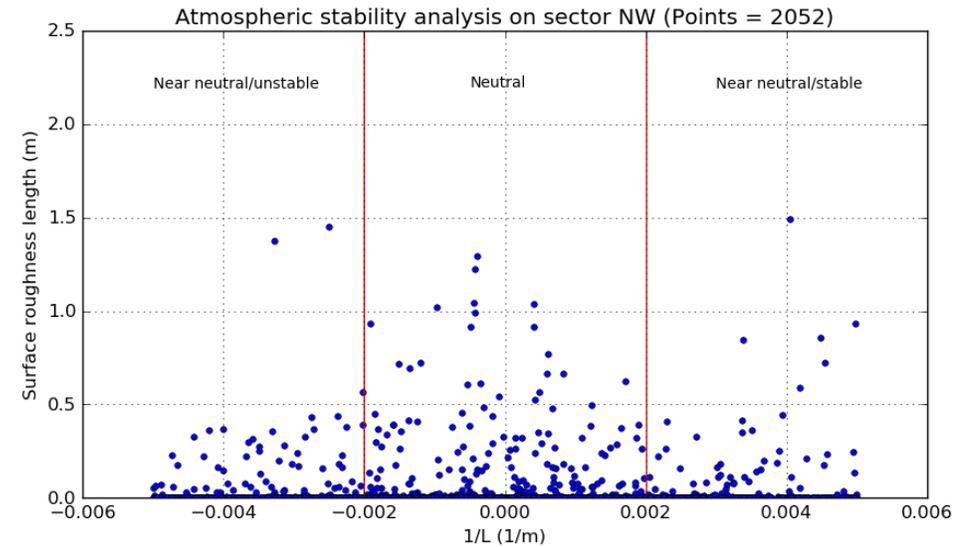
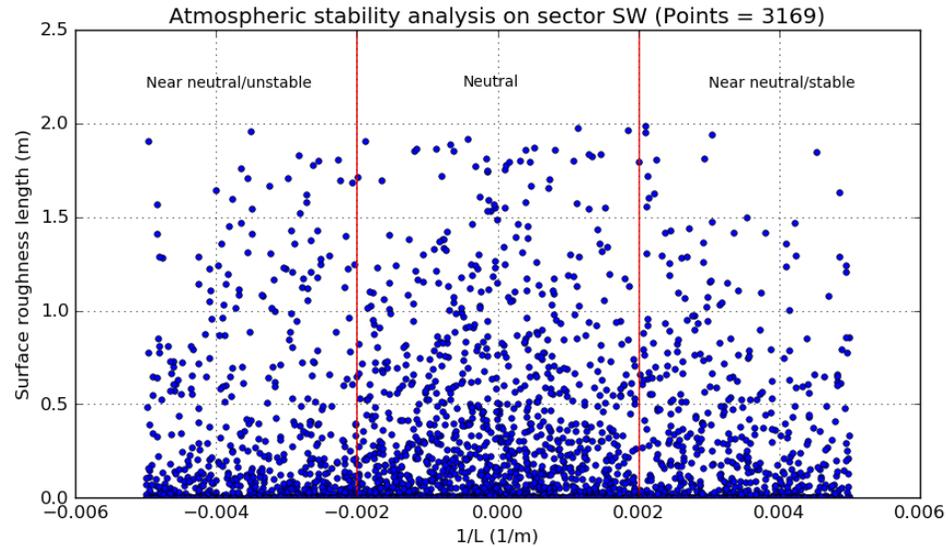


# On offshore high $z_0$ values: Wake effect



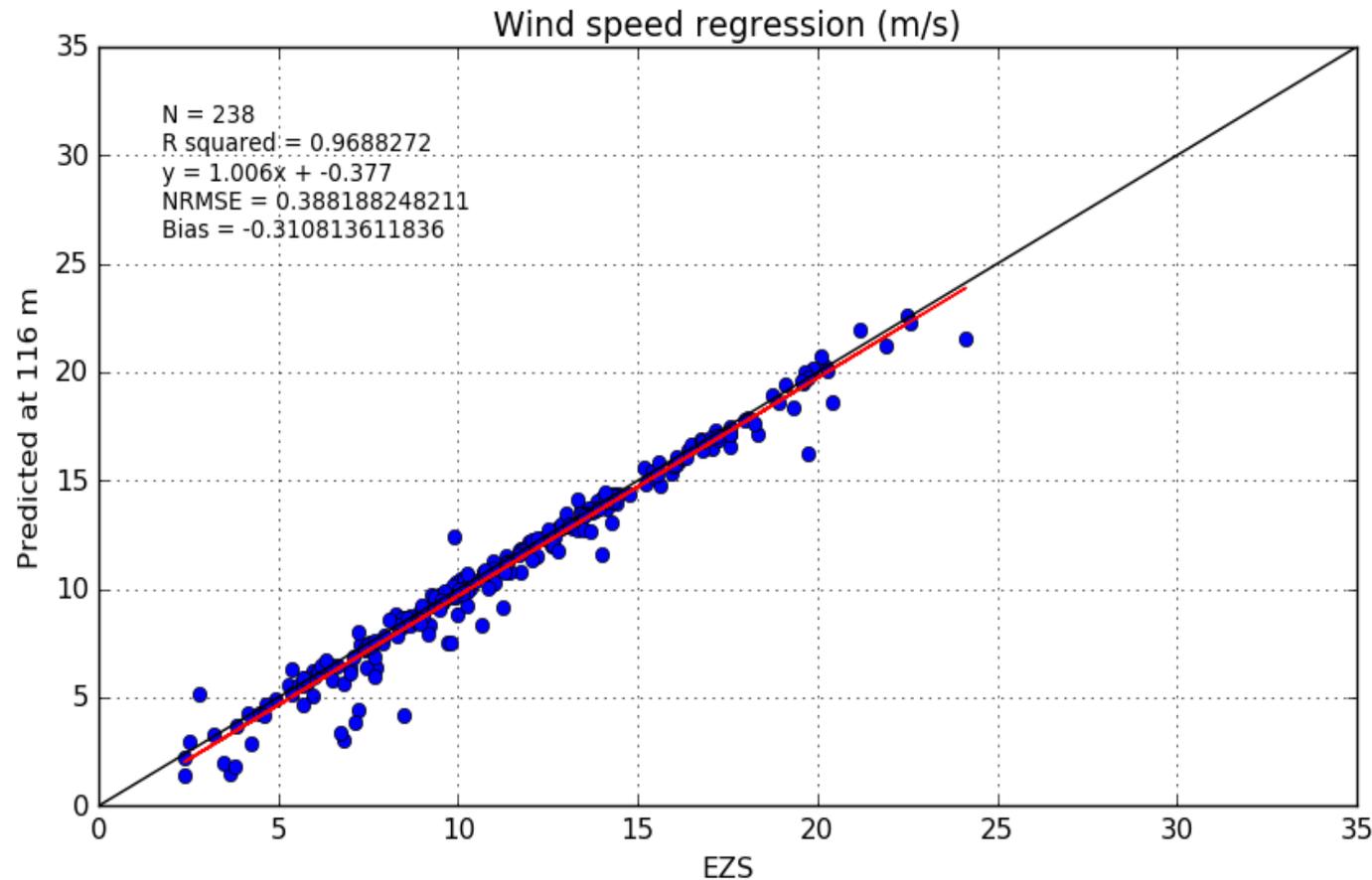
Analyses of surface roughness length under different stability conditions for the 3 sectors under a possible wake effect from wind turbines.

# On offshore high $z_0$ values: Wake effect



Analyses of surface roughness length under different stability conditions for the 3 assumed wake-free sectors.

# On offshore high $z_0$ values: Log law



$$U(z) = U(z_r) \left[ \frac{\ln(z/z_0)}{\ln(z_r/z_0)} \right]$$

→  $z_0$

$$u_* = \frac{\kappa(U_2 - U_1)}{\ln(z_2/z_1)}$$

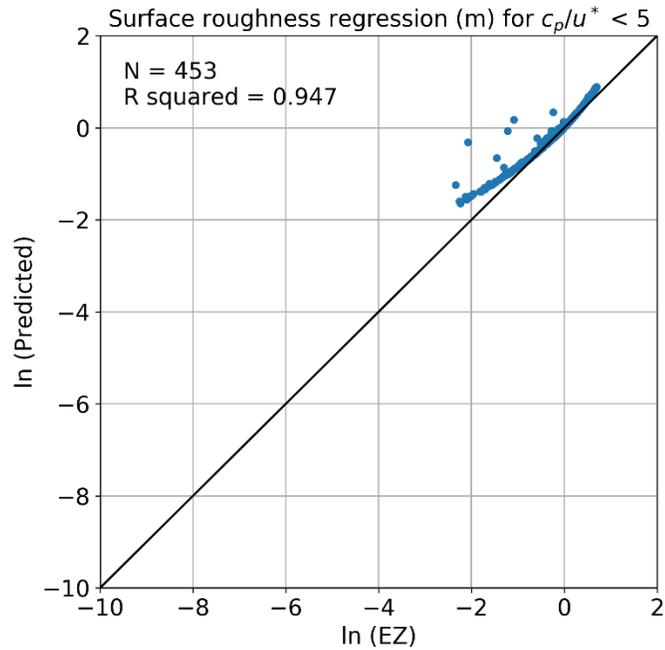
→  $u_*$

$$U(z) = \frac{U_*}{k} \left[ \ln\left(\frac{z}{z_0}\right) \right]$$

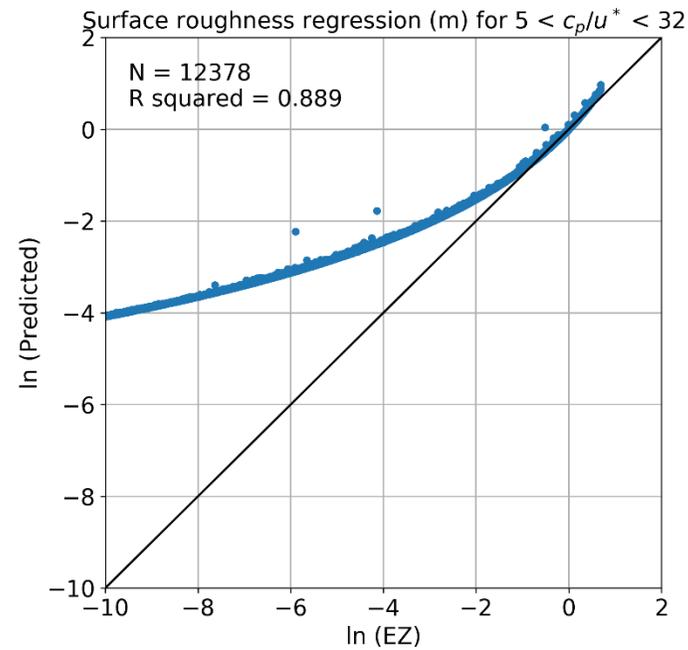
←

→  $U_{116}$

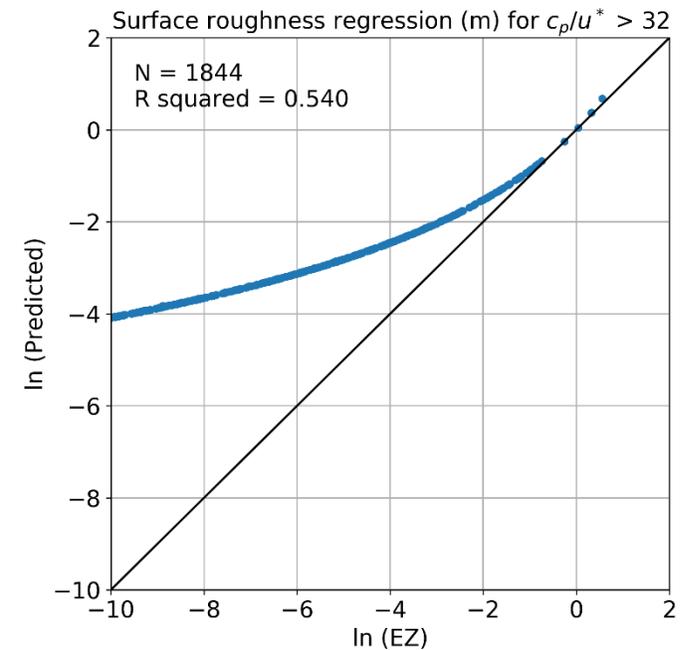
# On offshore high $z_0$ values: Sensibility analysis



Calm seas



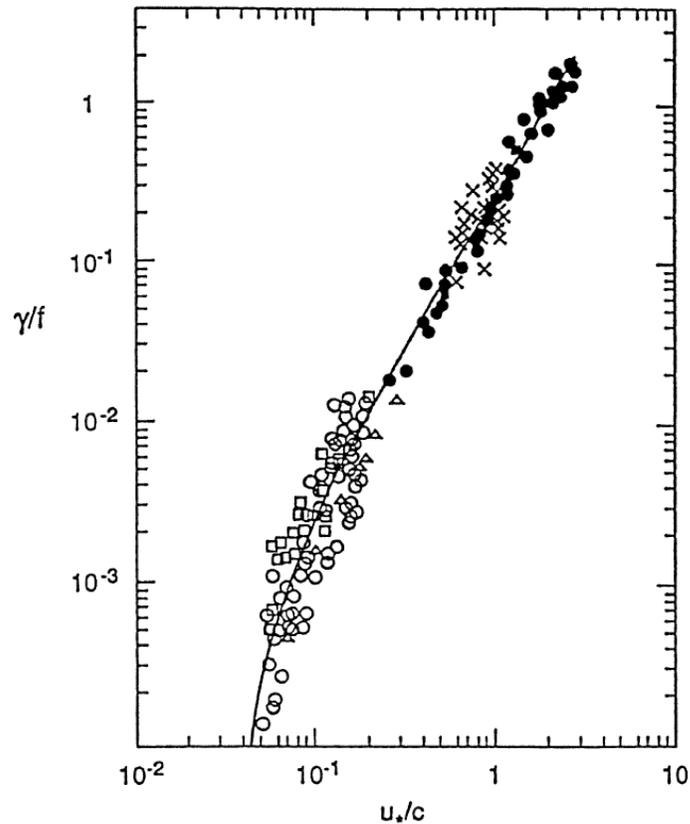
Growing  
seas



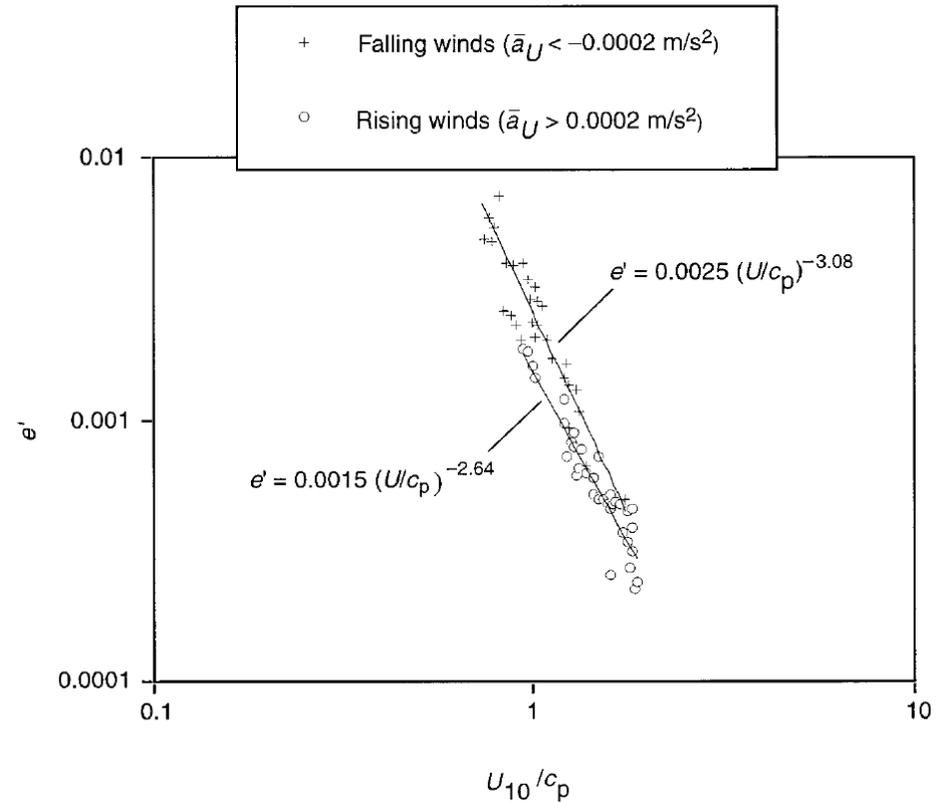
Decaying  
seas

**The younger the wave the rougher the sea**

# On offshore high $z_0$ values: Kinetic energy exchange



Observed non-dimensional wind wave growth rates (vertical axe) against the inverse wave age (horizontal axe). Open circles and squares are field data, others are laboratory data.  $\gamma$  represents the non-dimensional wind input growth rate,  $f$  is the wave frequency, and  $c$  is the phase speed. Source: Komen et al., 1994.



Non-dimensional wind energy ( $e'$ ) in falling and rising wind conditions against the inverse wave age. Source: J.L. Hanson, O.M. Phillips, 1999.

# New formulation: Lettau's equation

$C_d$  : Drag coefficient

$h^*$  : effective obstacle height

$s$  : silhouette or cross-section area

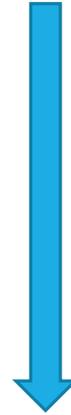
$n$  : number of obstacles

$A$  : area of the domain

$\theta$  : angle between wind and wave direction

$$z_0 = C_d h^* s (n/A)$$

Onshore



$$z_0 = \frac{u_*^2}{U_{10}^2} \frac{H_s^2}{L_p} |\cos \theta|$$

Offshore

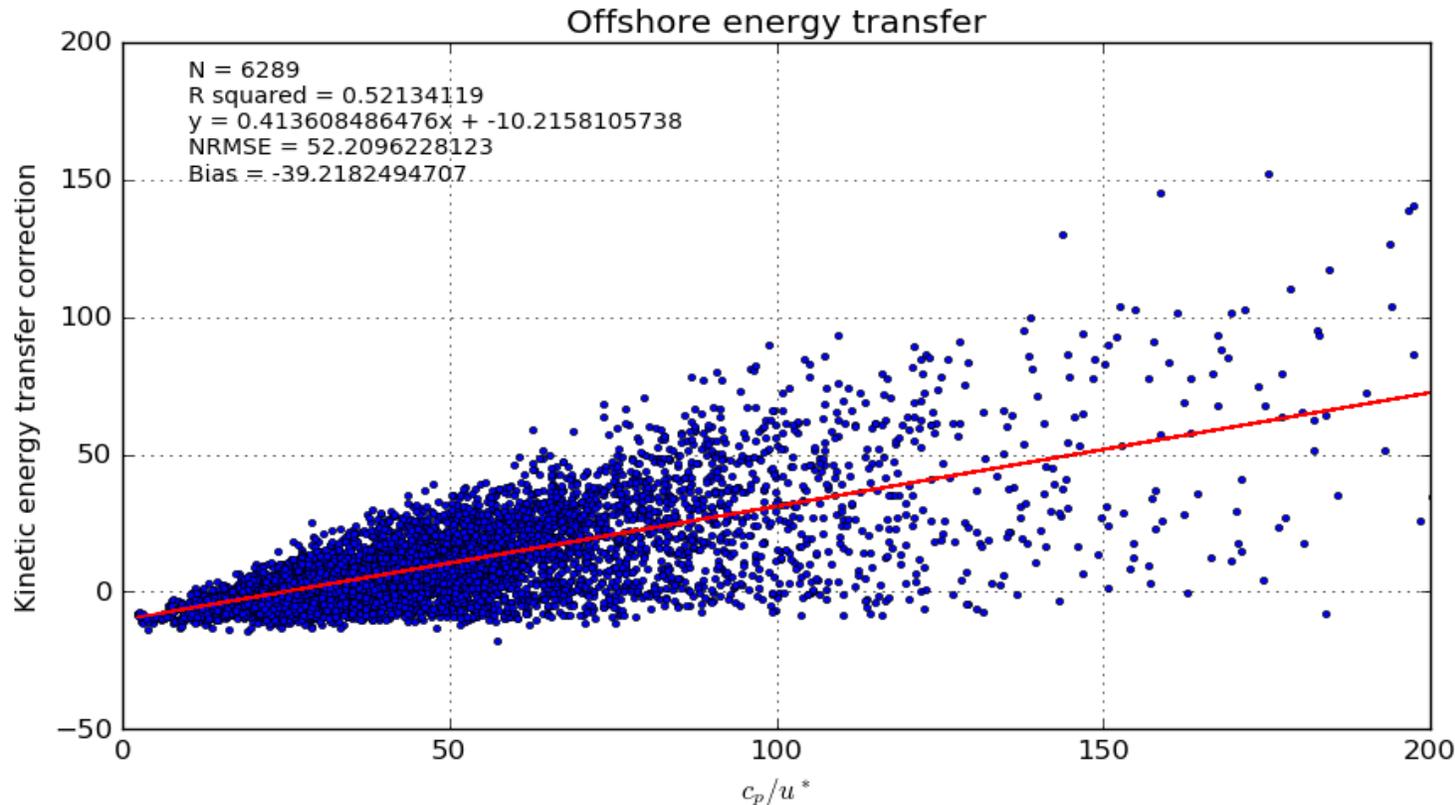
Assuming deep seas in absence of white capping and breaking waves

New formulation still agrees with the direct proportionality between  $z_0$  and  $u_*$  found by Charnock in 1952

# New formulation: Offshore log law

$$U(z) = \left(\frac{u_*}{\kappa}\right) \left[ \ln\left(\frac{z}{z_0}\right) + \Psi_s\left(\frac{z}{L_s}\right) + \varepsilon_k \left(\frac{c_p}{u_*}\right) \right]$$

Kinetic energy transfer correction between ocean and atmosphere (KETC)

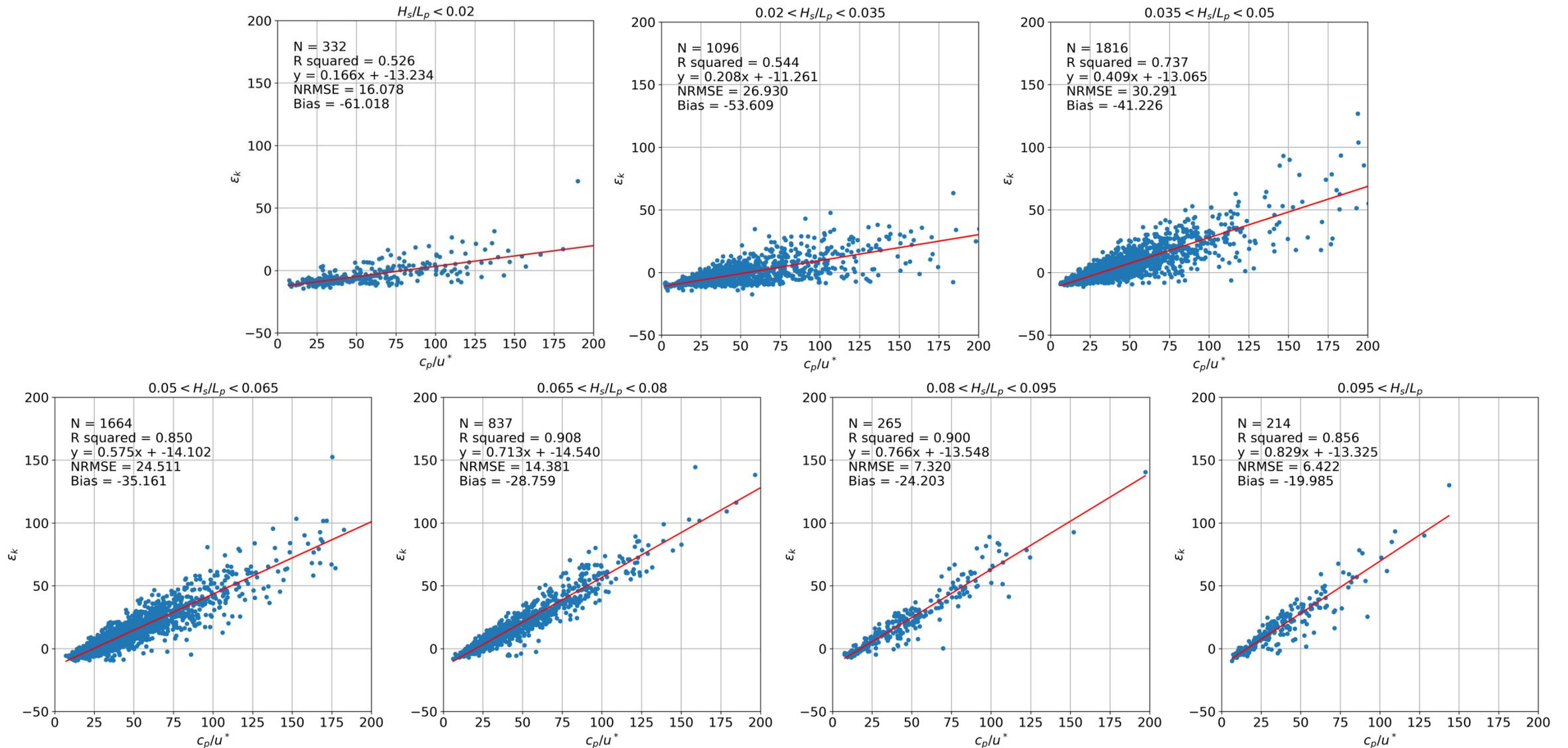


$$y = 0.414 \frac{c_p}{u_*} - 10.216$$

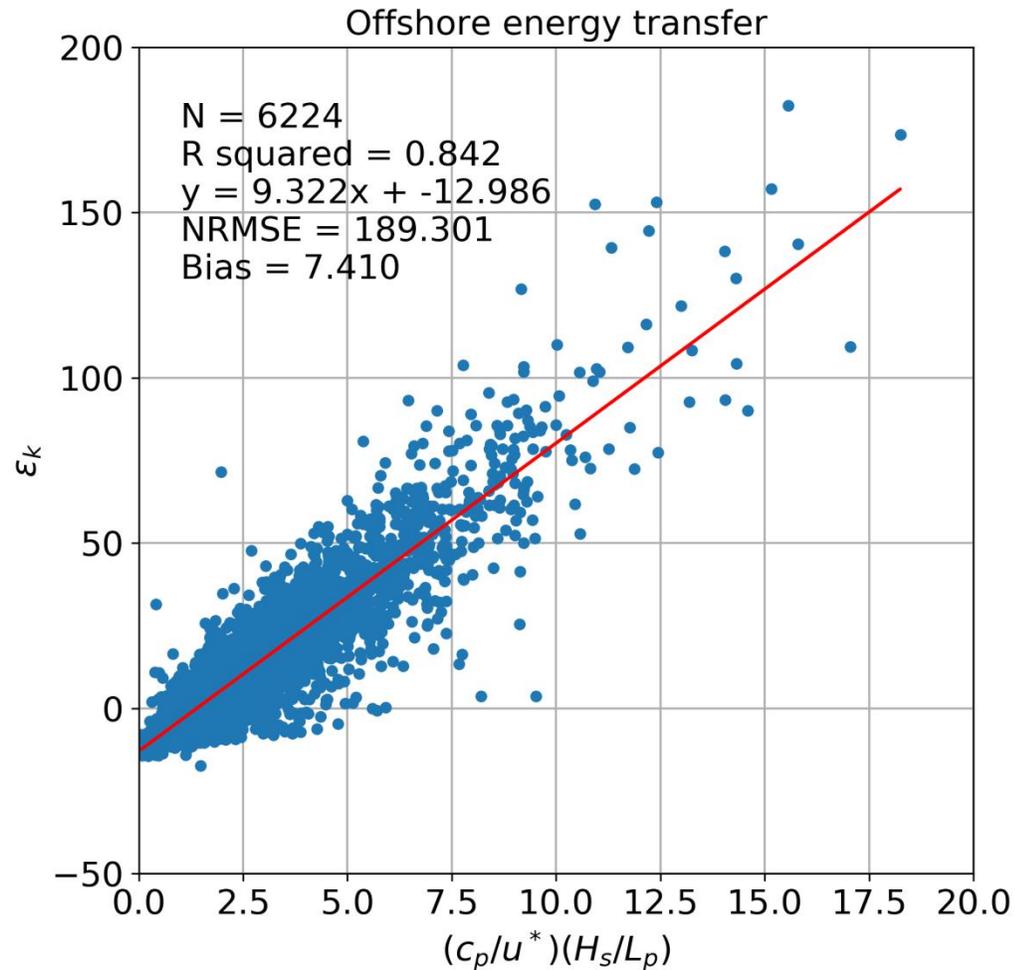
KETC	$c_p/u^*$	Sea type
< 0	< 24.68	Growing
≈ 0	= 24.68	Fully developed
> 0	> 24.68	Decaying

This wave age for fully developed seas agrees with literature where fully developed seas are meant to be found between  $22 - 35 \frac{c_p}{u^*}$

# New formulation: Offshore log law



# New formulation: Offshore log law



$$U(z) = \left(\frac{u_*}{\kappa}\right) \left[ \ln\left(\frac{z}{z_0}\right) + \Psi_s\left(\frac{z}{L_s}\right) + \epsilon_k \left(\frac{c_p}{u_*}, \frac{H_s}{L_p}\right) \right]$$

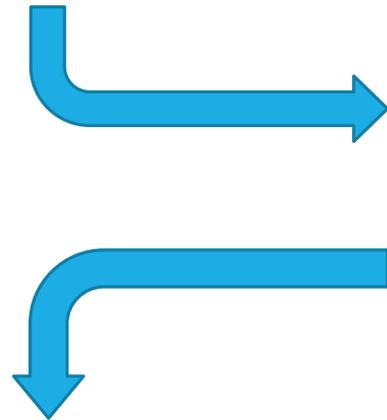
When  $z = 21$  metres

# New formulation: Offshore log law

## KETC at different heights

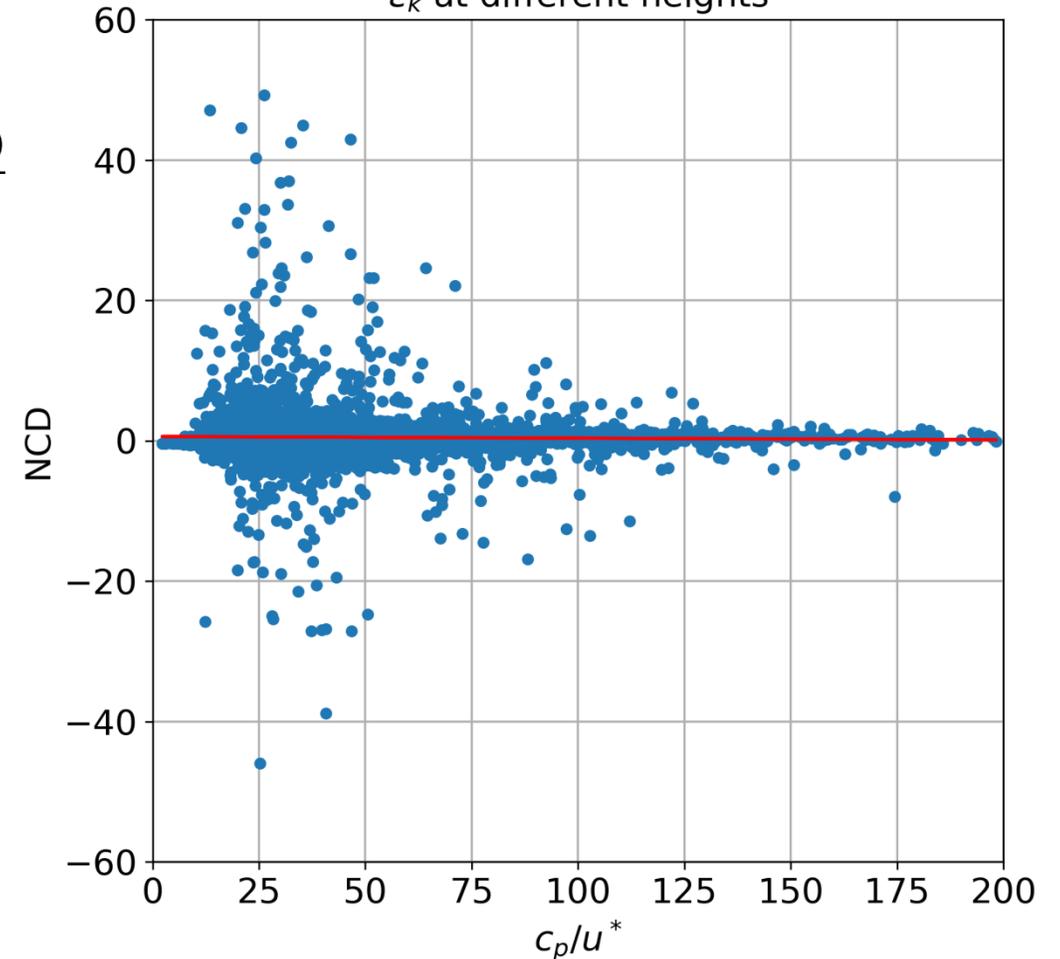
$$NCD = \frac{(KETC_{70} - KETC_{21}) + (KETC_{116} - KETC_{21}) + (KETC_{116} - KETC_{70})}{(KETC_{21} + KETC_{70} + KETC_{116})/3}$$

**NCD :**  
Normalised  
cumulative  
difference



$$U(z) = \left(\frac{u_*}{\kappa}\right) \left[ \ln\left(\frac{z}{z_0}\right) + \Psi_s\left(\frac{z}{L_s}\right) + \varepsilon_k\left(\frac{c_p}{u_*}, \frac{H_s}{L_p}, z\right) \right]$$

## $\varepsilon_k$ at different heights

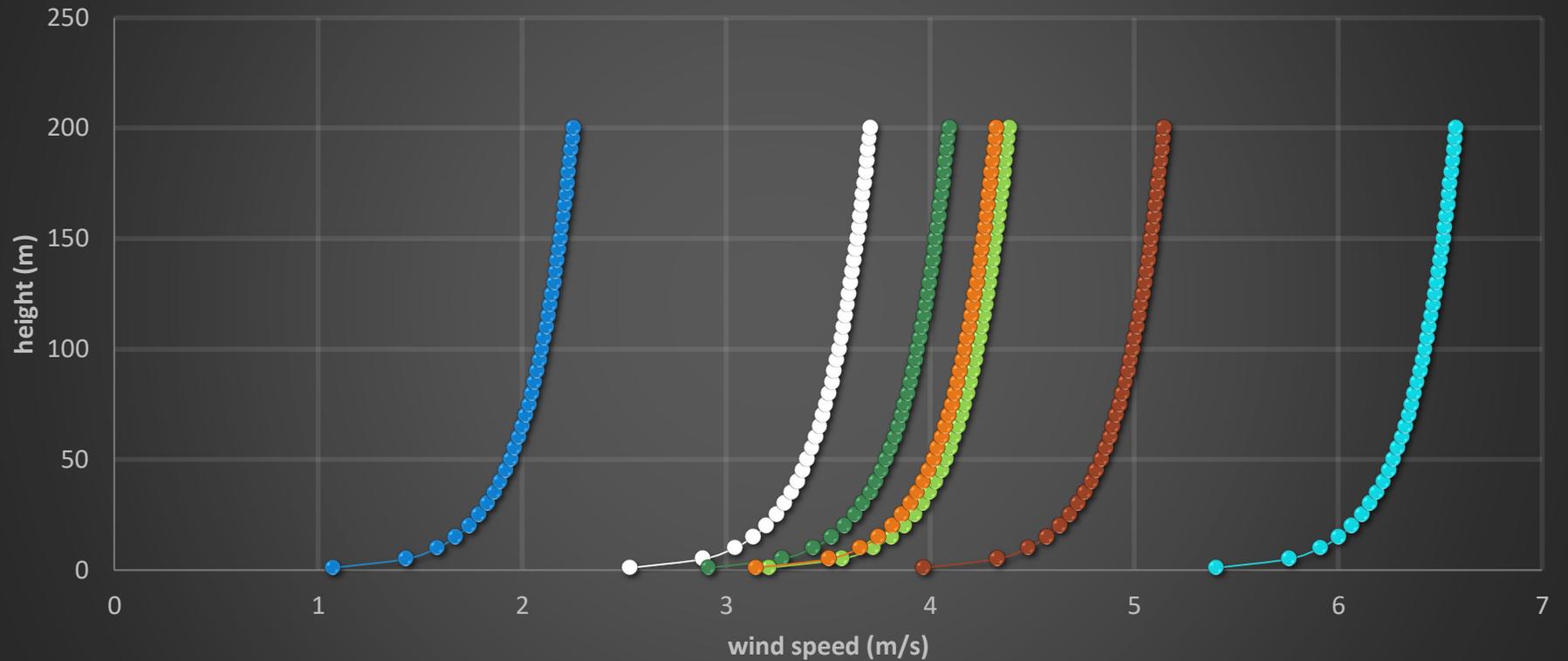


# Sensibility analysis

Average conditions at Egmond aan Zee under neutral conditions (excepting the angle)

$u^*$ (m/s)	0.089
$H_s$ (m)	1.14
$c_p/u^*$	24.67
$L_p$ (m)	18.24
$H_s/L_p$	0.0625
Angle	0
$z_0$ Rabaneda (m)	1.03005E-06
$z_0$ Charnock (m)	1.16272E-05

## Wind profiles under different sea conditions but neutral stability



—●— Control —●— Wave age = 3 —●— Wave age = 50 —●— Wave slope = 1/8 —●— Wave slope = 1/30 —●— Angle = 45 —●— Angle = 89

- The younger the waves, the rougher the seas.
- The offshore logarithmic law should differentiate between wind over a static surface (onshore) and wind over a non-static, fluidic surface (offshore).
- There is a kinetic energy exchange between wind and waves.
- Wave age has a dramatic impact on the wind profile. Wave slope and the angle of difference between wind and wave directions are significant but not as relevant as wave age.
- This energy exchange does not always affect equally at all heights. The younger the waves, the higher probability of unequal energy exchange at different heights.

- Study how the Kinetic Energy Transfer Correction varies with height.
- Repeat same study at different locations for validation.
- Analyze how much the pitch control of WT's is affected.
- Apply Computational Fluid Dynamics to:
  - Find the wave slope point where the wind behaves from single hill turbulent regime to consecutive hills near-laminar regime.
  - Analyze if the von Karman constant is in fact the sinus of the angle between the streak ejected from the turbulent flow near a wall parallel to the fluid motion, and the wall.
  - Analyze the momentum and energy transfer along the fetch which is long enough to reach fully developed waves.

**Are you interested in a further development of the offshore logarithmic law?**

**Will you be interested in including a variable sea surface roughness length inside WindSim for offshore applications?**



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Thank you

